

Mathematica 11.3 Integration Test Results

Test results for the 78 problems in "1.1.1.6 P(x) (a+b x)^m (c+d x)^n (e+f x)^p.m"

Problem 61: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sqrt{a + b x} \sqrt{c + d x} \sqrt{e + f x} (A + B x + C x^2) dx$$

Optimal (type 4, 1182 leaves, 10 steps):

$$\frac{1}{315 b^3 d^3 f^3} \left(2 (8 a^3 C d^3 f^3 + 3 a^2 b d^2 f^2 (C d e - c C f - 4 B d f) - 3 a b^2 d f^2 ((c^2 C - 7 A d^2) f + B d (d e - 2 c f)) - b^3 (C (16 d^3 e^3 - 3 c^2 d e f^2 - 8 c^3 f^3) + 3 d f (7 A d f (2 d e - c f) - B (8 d^2 e^2 - c d e f - 4 c^2 f^2))) \right) \sqrt{a + b x} \sqrt{c + d x} \sqrt{e + f x} - \frac{1}{105 b^2 d^2 f^3} 2 (7 b d f (b c C e + a C d e + a c C f - 3 A b d f) + (a d f - 4 b (d e + c f)) (2 a C d f - b (3 B d f - 2 C (d e + c f)))) \sqrt{a + b x} \sqrt{c + d x} (e + f x)^{3/2} - \frac{1}{21 b d^2 f^2} 2 (2 a C d f - b (3 B d f - 2 C (d e + c f))) \sqrt{a + b x} (c + d x)^{3/2} (e + f x)^{3/2} + \frac{2 C (a + b x)^{3/2} (c + d x)^{3/2} (e + f x)^{3/2}}{9 b d f} - \frac{1}{315 b^4 d^{7/2} f^4 \sqrt{c + d x} \sqrt{\frac{b(e+fx)}{be-af}}} 2 \sqrt{-bc+ad} (16 a^4 C d^4 f^4 - 8 a^3 b d^3 f^3 (C d e + c C f + 3 B d f) + 3 a^2 b^2 d^2 f^2 (d f (5 B d e + 5 B c f + 14 A d f) - 2 C (d^2 e^2 - c d e f + c^2 f^2)) - a b^3 d f (C (8 d^3 e^3 - 6 c d^2 e^2 f - 6 c^2 d e f^2 + 8 c^3 f^3) + 3 d f (14 A d f (d e + c f) - B (5 d^2 e^2 - 6 c d e f + 5 c^2 f^2))) + b^4 (2 C (8 d^4 e^4 - 4 c d^3 e^3 f - 3 c^2 d^2 e^2 f^2 - 4 c^3 d e f^3 + 8 c^4 f^4) + 3 d f (14 A d f (d^2 e^2 - c d e f + c^2 f^2) - B (8 d^3 e^3 - 5 c d^2 e^2 f - 5 c^2 d e f^2 + 8 c^3 f^3)))) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] - \frac{1}{315 b^4 d^{7/2} f^4 \sqrt{c+dx} \sqrt{e+fx}} 2 \sqrt{-bc+ad} (be-af) (de-cf) \left(8 a^3 C d^3 f^3 + 3 a^2 b d^2 f^2 (C d e - c C f - 4 B d f) - 3 a b^2 d f^2 ((c^2 C - 7 A d^2) f + B d (d e - 2 c f)) - b^3 (C (16 d^3 e^3 - 3 c^2 d e f^2 - 8 c^3 f^3) + 3 d f (7 A d f (2 d e - c f) - B (8 d^2 e^2 - c d e f - 4 c^2 f^2))) \right) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right]$$

Result (type 4, 11933 leaves):

$$\sqrt{a + b x} \sqrt{c + d x} \sqrt{e + f x} \left(\frac{1}{315 b^3 d^3 f^3} 2 (8 b^3 C d^3 e^3 - 3 b^3 c C d^2 e^2 f - 12 b^3 B d^3 e^2 f - 3 a b^2 C d^3 e^2 f - 3 b^3 c^2 C d e f^2 + 6 b^3 B c d^2 e f^2 + 2 a b^2 c C d^2 e f^2 + 21 A b^3 d^3 e f^2 + 6 a b^2 B d^3 e f^2 - 3 a^2 b C d^3 e f^2 + 8 b^3 c^3 C f^3 - 12 b^3 B c^2 d f^3 - 3 a b^2 c^2 C d f^3 + 21 A b^3 c d^2 f^3 + 6 a b^2 B c d^2 f^3 - 3 a^2 b c C d^2 f^3 + 21 a A b^2 d^3 f^3 - 12 a^2 b B d^3 f^3 + 8 a^3 C d^3 f^3) + \frac{1}{315 b^2 d^2 f^2} 2 (-6 b^2 C d^2 e^2 + 2 b^2 c C d e f + 9 b^2 B d^2 e f + 2 a b C d^2 e f - 6 b^2 c^2 C f^2 + 9 b^2 B c d f^2 + 2 a b c C d f^2 + 63 A b^2 d^2 f^2 + 9 a b B d^2 f^2 - 6 a^2 C d^2 f^2) x + \frac{2 (b C d e + b c C f + 9 b B d f + a C d f) x^2}{63 b d f} + \frac{2 C x^3}{9} \right) -$$

$$\frac{1}{315 b^5 d^3 f^3} 2 \left(\frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right.$$

$$(16 b^4 C d^4 e^4 - 8 b^4 c C d^3 e^3 f - 24 b^4 B d^4 e^3 f - 8 a b^3 C d^4 e^3 f - 6 b^4 c^2 C d^2 e^2 f^2 + 15 b^4 B c d^3 e^2 f^2 + 6 a b^3 c C d^3 e^2 f^2 + 42 A b^4 d^4 e^2 f^2 + 15 a b^3 B d^4 e^2 f^2 - 6 a^2 b^2 C d^4 e^2 f^2 - 8 b^4 c^3 C d e f^3 + 15 b^4 B c^2 d^2 e f^3 + 6 a b^3 c^2 C d^2 e f^3 - 42 A b^4 c d^3 e f^3 - 18 a b^3 B c d^3 e f^3 + 6 a^2 b^2 c C d^3 e f^3 - 42 a A b^3 d^4 e f^3 + 15 a^2 b^2 B d^4 e f^3 - 8 a^3 b C d^4 e f^3 + 16 b^4 c^4 C f^4 - 24 b^4 B c^3 d f^4 - 8 a b^3 c^3 C d f^4 + 42 A b^4 c^2 d^2 f^4 + 15 a b^3 B c^2 d^2 f^4 - 6 a^2 b^2 c^2 C d^2 f^4 - 42 a A b^3 c d^3 f^4 + 15 a^2 b^2 B c d^3 f^4 - 8 a^3 b c C d^3 f^4 + 42 a^2 A b^2 d^4 f^4 - 24 a^3 b B d^4 f^4 + 16 a^4 C d^4 f^4) (a+bx)^{3/2}$$

$$\left. \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) - \frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right.$$

$$\left. (-bc+ad) (-be+af) (a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \right.$$

$$\left. \left(\left(16 i b^4 C d^4 e^4 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(8 i b^4 c C d^3 \right.$$

$$\left. e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(24 i b^4 B d^4 e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(8 i a b^3 C d^4 \right.$$

$$e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(6 i b^4 c^2 C \right.$$

$$d^2 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i b^4 B c \right.$$

$$d^3 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(6 i a b^3 c C \right.$$

$$d^3 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(42 i A b^4 d^4 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i a b^3 B \right.$$

$$d^4 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(6 i a^2 b^2 C \right.$$

$$d^4 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i b^4 c^3 C d e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(15 i b^4 B c^2 d^2 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a b^3 c^2 C d^2 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(42 i A b^4 c d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(18 i a b^3 B c d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a^2 b^2 c C d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \\
 \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 \left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 \left(42 i a A b^3 d^4 e f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) \\
 \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \\
 \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 \left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 \left(15 i a^2 b^2 B d^4 e f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) \\
 \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(8 i a^3 b c d^4 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(16 i b^4 c^4 C f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(24 i b^4 B c^3 d f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.
 \end{aligned}$$

$$\left(\frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(8 \text{i} a b^3 c^3 C d f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \right.$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \right.$$

$$\left. \left(42 \text{i} A b^4 c^2 d^2 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \right.$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \right.$$

$$\left. \left(15 \text{i} a b^3 B c^2 d^2 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right) \right)$$

$$\left(\begin{aligned} & \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \\ & \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \end{aligned} \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(6 \text{i} a^2 b^2 c^2 d^2 f^5 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) -$$

$$\left(\begin{aligned} & \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \\ & \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \end{aligned} \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(42 \text{i} a A b^3 c d^3 f^5 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) -$$

$$\left(\begin{aligned} & \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \end{aligned} \right)$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(15 \text{i} a^2 b^2 B c d^3 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \right. \\
 & \left. \left. \left. \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right)\right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(8 \text{i} a^3 b c C d^3 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\left(42 \, i \, a^2 \, A \, b^2 \, d^4 \, f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(24 \, i \, a^3 \, b \, B \, d^4 \, f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(16 \, i \, a^4 \, C \, d^4 \, f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i b^3 C d^4 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(3 i b^3 c C d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(12 i b^3 B d^4 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(3 i a b^2 C d^4 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(3 \, i \, b^3 \, c^2 \, C \, d^2 \, e \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(6 \, i \, b^3 \, B \, c \, d^3 \, e \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(21 \, i \, A \, b^3 \, d^4 \, e \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(3 \, i \, a \, b^2 \, B \, d^4 \, e \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(8 \, i \, b^3 \, c^3 \, C \, d \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(12 \, i \, b^3 \, B \, c^2 \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(3 \, i \, a \, b^2 \, c^2 \, C \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(21 \, i \, A \, b^3 \, c \, d^3 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /
 \end{aligned}$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(3 \, i \, a \, b^2 \, B \, c \, d^3 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(42 \, i \, a \, A \, b^2 \, d^4 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(24 \, i \, a^2 \, b \, B \, d^4 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \right.$$

$$\left. \left(16 \, i \, a^3 \, C \, d^4 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 62: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} \sqrt{e+fx} (A+Bx+Cx^2)}{\sqrt{a+bx}} dx$$

Optimal (type 4, 774 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{105 b^3 d^2 f^2} 2 (5 b d f (3 a C (d e + c f) + b (c C e - 7 A d f)) - \\ & \quad (2 b d e - b c f + 4 a d f) (6 a C d f - b (7 B d f - 4 C (d e + c f)))) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} - \\ & \quad \frac{2 (6 a C d f - b (7 B d f - 4 C (d e + c f))) \sqrt{a+bx} \sqrt{c+dx} (e+fx)^{3/2}}{35 b^2 d f^2} + \\ & \quad \frac{2 C \sqrt{a+bx} (c+dx)^{3/2} (e+fx)^{3/2}}{7 b d f} - \frac{1}{105 b^4 d^{5/2} f^3 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}} \\ & \quad 2 \sqrt{-bc+ad} \left(3 b d f (5 b c f (3 a C (d e + c f) + b (c C e - 7 A d f)) - \right. \\ & \quad \quad (b c e + a d e + 3 a c f) (6 a C d f - b (7 B d f - 4 C (d e + c f)))) + \\ & \quad \quad \left. 2 \left(\frac{b d e}{2} - (b c + a d) f \right) (5 b d f (3 a C (d e + c f) + b (c C e - 7 A d f)) - \right. \\ & \quad \quad \left. (2 b d e - b c f + 4 a d f) (6 a C d f - b (7 B d f - 4 C (d e + c f)))) \right) \\ & \quad \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] - \\ & \quad \left(2 \sqrt{-bc+ad} (be-af) (de-cf) (24 a^2 C d^2 f^2 + a b d f (13 C d e - 5 c C f - 28 B d f)) - \right. \\ & \quad \quad \left. b^2 (7 d f (2 B d e - B c f - 5 A d f) - C (8 d^2 e^2 - c d e f - 4 c^2 f^2)) \right) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \\ & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] \right) / (105 b^4 d^{5/2} f^3 \sqrt{c+dx} \sqrt{e+fx}) \end{aligned}$$

Result (type 4, 7297 leaves):

$$\begin{aligned} & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\ & \left(\frac{1}{105 b^3 d^2 f^2} 2 (-4 b^2 C d^2 e^2 + 2 b^2 c C d e f + 7 b^2 B d^2 e f - 5 a b C d^2 e f - 4 b^2 c^2 C f^2 + \right. \\ & \quad \left. 7 b^2 B c d f^2 - 5 a b c C d f^2 + 35 A b^2 d^2 f^2 - 28 a b B d^2 f^2 + 24 a^2 C d^2 f^2) + \right. \\ & \quad \left. \frac{2 (b C d e + b c C f + 7 b B d f - 6 a C d f) x + \frac{2 C x^2}{7 b}}{35 b^2 d f} \right) - \end{aligned}$$

$$\frac{1}{105 b^5 d^2 f^2} 2 \left(\frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right.$$

$$\begin{aligned} & (-8 b^3 C d^3 e^3 + 5 b^3 c C d^2 e^2 f + 14 b^3 B d^3 e^2 f - 9 a b^2 C d^3 e^2 f + 5 b^3 c^2 C d e f^2 - \\ & 14 b^3 B c d^2 e f^2 + 8 a b^2 c C d^2 e f^2 - 35 A b^3 d^3 e f^2 + 21 a b^2 B d^3 e f^2 - 16 a^2 b C d^3 e f^2 - \\ & 8 b^3 c^3 C f^3 + 14 b^3 B c^2 d f^3 - 9 a b^2 c^2 C d f^3 - 35 A b^3 c d^2 f^3 + 21 a b^2 B c d^2 f^3 - \\ & 16 a^2 b c C d^2 f^3 + 70 a A b^2 d^3 f^3 - 56 a^2 b B d^3 f^3 + 48 a^3 C d^3 f^3) (a+bx)^{3/2} \\ & \left. \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) + \frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right. \end{aligned}$$

$$\left. (-bc+ad) (-be+af) (a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \right.$$

$$\left. \left(\left(8 i b^3 C d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right) - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(5 i b^3 c C d^2 \right.$$

$$\left. e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right) - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\begin{aligned}
 & \left(14 \, i \, b^3 \, B \, d^3 \, e^2 \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(9 \, i \, a \, b^2 \, C \, d^3 \right. \\
 & \left. e^2 \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(5 \, i \, b^3 \, c^2 \, C \, d \, e \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(14 \, i \, b^3 \, B \, c \right.
 \end{aligned}$$

$$\begin{aligned}
 & d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(8 i a b^2 c C \right. \\
 & d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(35 i A b^3 d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(21 i a b^2 B \right.
 \end{aligned}$$

$$\begin{aligned}
 & d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(16 i a^2 b c d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(8 i b^3 c^3 C f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(14 i b^3 B c^2 d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(9 i a b^2 c^2 C d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(35 i A b^3 c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(21 i a b^2 B c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(16 i a^2 b c C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(70 i a A b^2 d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(56 \text{i} a^2 b B d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(48 \text{i} a^3 C d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(4 \text{i} b^2 C d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)}\right) + \left(2 \text{i} b^2 c C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}}\right)$$

$$\left.\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)}\right) + \left(7 \text{i} b^2 B d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}}\right)$$

$$\left.\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)}\right) - \left(8 \text{i} a b C d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}}\right)$$

$$\left.\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)}\right) - \left(4 \text{i} b^2 c^2 C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}}\right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(7i b^2 B c d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(8i a b c C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(70i A b^2 d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(56i a b B d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(48 i a^2 c d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right/$$

$$\left(\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 63: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} \sqrt{e+fx} (A+Bx+Cx^2)}{(a+bx)^{3/2}} dx$$

Optimal (type 4, 706 leaves, 9 steps):

$$\begin{aligned} & \left(2 (24 a^2 C d f^2 - a b f (7 C d e + c C f + 20 B d f)) + b^2 (5 d f (B e + 3 A f) - C e (2 d e - c f)) \right) \\ & \quad \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \Big/ (15 b^3 d f (b e - a f)) + \\ & \left(2 (6 a^2 C d f + b^2 (c C e + 5 A d f) - a b (C d e + c C f + 5 B d f)) \sqrt{a+bx} \sqrt{c+dx} (e+fx)^{3/2} \Big/ \right. \\ & \quad \left. (5 b^2 (b c - a d) f (b e - a f)) - \frac{2 (A b^2 - a (b B - a C)) (c+dx)^{3/2} (e+fx)^{3/2}}{b (b c - a d) (b e - a f) \sqrt{a+bx}} + \right. \\ & \left. \left(2 \sqrt{-bc+ad} (48 a^2 C d^2 f^2 - 8 a b d f (C d e + c C f + 5 B d f)) + \right. \right. \\ & \quad \left. \left. b^2 (5 d f (B d e + B c f + 6 A d f) - 2 C (d^2 e^2 - c d e f + c^2 f^2)) \right) \sqrt{\frac{b (c+dx)}{b c - a d}} \sqrt{e+fx} \right. \\ & \quad \left. \text{EllipticE} \left[\text{ArcSin} \left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}} \right], \frac{(b c - a d) f}{d (b e - a f)} \right] \right) \Big/ \left(15 b^4 d^{3/2} f^2 \sqrt{c+dx} \sqrt{\frac{b (e+fx)}{b e - a f}} \right) - \\ & \left(2 \sqrt{-bc+ad} (d e - c f) (24 a^2 C d f^2 - a b f (7 C d e + c C f + 20 B d f)) + \right. \\ & \quad \left. b^2 (5 d f (B e + 3 A f) - C e (2 d e - c f)) \sqrt{\frac{b (c+dx)}{b c - a d}} \sqrt{\frac{b (e+fx)}{b e - a f}} \right. \\ & \quad \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}} \right], \frac{(b c - a d) f}{d (b e - a f)} \right] \right) \Big/ (15 b^4 d^{3/2} f^2 \sqrt{c+dx} \sqrt{e+fx}) \end{aligned}$$

Result (type 4, 9487 leaves):

$$\begin{aligned} & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\ & \left(\frac{2 (b C d e + b c C f + 5 b B d f - 9 a C d f)}{15 b^3 d f} + \frac{2 C x}{5 b^2} - \frac{2 (A b^2 - a b B + a^2 C)}{b^3 (a+bx)} \right) + \frac{1}{15 b^5 d f} \\ & 2 \left(\left((-2 b^2 C d^2 e^2 + 2 b^2 c C d e f + 5 b^2 B d^2 e f - 8 a b C d^2 e f - 2 b^2 c^2 C f^2 + 5 b^2 B c d f^2 - 8 a b c C d f^2 + \right. \right. \\ & \quad \left. \left. 30 A b^2 d^2 f^2 - 40 a b B d^2 f^2 + 48 a^2 C d^2 f^2) (a+bx)^{3/2} \left(d + \frac{b c}{a+bx} - \frac{a d}{a+bx} \right) \right. \right. \\ & \quad \left. \left. \left(f + \frac{b e}{a+bx} - \frac{a f}{a+bx} \right) \right) \Big/ \left(d f \sqrt{c + \frac{(a+bx) \left(d - \frac{a d}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left(f - \frac{a f}{a+bx} \right)}{b}} \right) + \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \\
 & (a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx}\right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx}\right)} \\
 & \left(\left(2 i b^4 c C d^2 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Big/ \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 i a b^3 C d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Big/ \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(2 i b^4 c^2 C d \right. \\
 & \left. e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right.
 \end{aligned}$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(5 \text{i} b^4 B c d^2 \right. \right.$$

$$\left. e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(8 \text{i} a b^3 c C \right. \right.$$

$$\left. d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(5 \text{i} a b^3 B d^3 \right. \right.$$

$$\begin{aligned}
 & e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(6 i a^2 b^2 c d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(2 i b^4 c^3 C e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(5 i b^4 B c^2 d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(8 i a b^3 c^2 C d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(30 i A b^4 c d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)
 \end{aligned}$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(50 i a b^3 B c d^2 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(66 i a^2 b^2 c C d^2 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(30 i a A b^3 d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) - \right)$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(45 i a^2 b^2 B d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) - \right)$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(56 i a^3 b C d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 i a b^3 c^3 C f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(5 i a b^3 B c^2 d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(6 i a^2 b^2 c^2 c d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(30 i a A b^3 c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(45 i a^2 b^2 B c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(56 i a^3 b c C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\begin{aligned}
 & \left(30 \, i \, a^2 \, A \, b^2 \, d^3 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(40 \, i \, a^3 \, b \, B \, d^3 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(48 \, i \, a^4 \, C \, d^3 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(i b^3 c C d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\ \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(i a b^2 C d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\ \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(i b^3 c^2 C d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\ \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(10 i b^3 B c d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\ \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left[16 i a b^2 c C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left[15 i A b^3 d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left[25 i a b^2 B d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left[32 i a^2 b C d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(i a b^2 c^2 C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(15 i A b^3 c d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(25 i a b^2 B c d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \right.$$

$$\left. \left(32 i a^2 b c C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \right.$$

$$\left. \left. \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(30 i a A b^2 d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right)$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(40 i a^2 b B d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right)$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(48 i a^3 C d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 64: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} \sqrt{e+fx} (A+Bx+Cx^2)}{(a+bx)^{5/2}} dx$$

Optimal (type 4, 687 leaves, 9 steps):

$$\begin{aligned}
 & \left(2 (8a^2 C d f + b^2 (c C e + 3 B c f + A d f) - a b (C d e + 7 c C f + 4 B d f)) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \right) / \\
 & \left(3 b^3 (b c - a d) (b e - a f) \right) - \frac{2 (b B - 2 a C) \sqrt{c+dx} (e+fx)^{3/2}}{b^2 (b e - a f) \sqrt{a+bx}} - \\
 & \frac{2 (A b^2 - a (b B - a C)) (c+dx)^{3/2} (e+fx)^{3/2}}{3 b (b c - a d) (b e - a f) (a+bx)^{3/2}} + \\
 & \left(2 (16 a^3 C d^2 f^2 - 8 a^2 b d f (B d f + 2 C (d e + c f)) - b^3 (c^2 C e f + A d^2 e f + c d (C e^2 + 6 B e f + A f^2)) + \right. \\
 & \quad \left. a b^2 (d f (7 B d e + 7 B c f + 2 A d f) + C (d^2 e^2 + 16 c d e f + c^2 f^2)) \right) \\
 & \left. \sqrt{\frac{b (c+dx)}{b c - a d}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-b c + a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right] \right) / \\
 & \left(3 b^4 \sqrt{d} \sqrt{-b c + a d} f (b e - a f) \sqrt{c+dx} \sqrt{\frac{b (e+fx)}{b e - a f}} \right) + \\
 & \left(2 (d e - c f) (8 a^2 C d f + b^2 (c C e + 3 B c f + A d f) - a b (C d e + 7 c C f + 4 B d f)) \right. \\
 & \quad \left. \sqrt{\frac{b (c+dx)}{b c - a d}} \sqrt{\frac{b (e+fx)}{b e - a f}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-b c + a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right] \right) / \\
 & \left(3 b^4 \sqrt{d} \sqrt{-b c + a d} f \sqrt{c+dx} \sqrt{e+fx} \right)
 \end{aligned}$$

Result(type 4, 5831 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\
 & \left(\frac{2 C}{3 b^3} - \frac{2 (A b^2 - a b B + a^2 C)}{3 b^3 (a+bx)^2} - (2 (3 b^3 B c e - 6 a b^2 c C e + A b^3 d e - 4 a b^2 B d e + 7 a^2 b C d e + \right. \\
 & \quad \left. A b^3 c f - 4 a b^2 B c f + 7 a^2 b c C f - 2 a A b^2 d f + 5 a^2 b B d f - 8 a^3 C d f) \right) / \\
 & \left(3 b^3 (b c - a d) (b e - a f) (a+bx) \right) \Bigg) - \frac{1}{3 b^5 (b c - a d) (b e - a f)} \\
 & 2 \left(\left((-b^3 c C d e^2 + a b^2 C d^2 e^2 - b^3 c^2 C e f - 6 b^3 B c d e f + 16 a b^2 c C d e f - A b^3 d^2 e f + 7 a b^2 B d^2 e f - \right. \right. \\
 & \quad \left. \left. 16 a^2 b C d^2 e f + a b^2 c^2 C f^2 - A b^3 c d f^2 + 7 a b^2 B c d f^2 - 16 a^2 b c C d f^2 + 2 a A b^2 d^2 f^2 - \right. \right. \\
 & \quad \left. \left. 8 a^2 b B d^2 f^2 + 16 a^3 C d^2 f^2) (a+bx)^{3/2} \left(d + \frac{b c}{a+bx} - \frac{a d}{a+bx} \right) \left(f + \frac{b e}{a+bx} - \frac{a f}{a+bx} \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(d f \sqrt{c + \frac{(a+bx) \left(d - \frac{ad}{a+bx}\right)}{b}} \sqrt{e + \frac{(a+bx) \left(f - \frac{af}{a+bx}\right)}{b}} \right) + \\
 & \frac{1}{d f \sqrt{c + \frac{(a+bx) \left(d - \frac{ad}{a+bx}\right)}{b}} \sqrt{e + \frac{(a+bx) \left(f - \frac{af}{a+bx}\right)}{b}}} \\
 & (-bc+ad) (-be+af) (a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx}\right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx}\right)} \\
 & \left(\left(i b^3 c d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(i a b^2 C d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(i b^3 c^2 C e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 \text{i} b^3 B c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(16 \text{i} a b^2 c$$

$$C d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(\text{i} A b^3 d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(7 i a b^2 B d^2 e f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(16 i a^2 b c$$

$$d^2 e f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a b^2 c^2 C f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i A b^3 c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(7 i a b^2 B c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(16 i a^2 b c C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 \text{i a A b}^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 \text{i a}^2 b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(16 \text{i a}^3 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i b^2 c C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i b^2 B d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i a b C d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i b^2 B c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i a b c C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i A b^2 d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i a b B d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(16 i a^2 C d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] \left/ \left(\sqrt{-\frac{bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 65: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} \sqrt{e+fx} (A+Bx+Cx^2)}{(a+bx)^{7/2}} dx$$

Optimal (type 4, 964 leaves, 9 steps):

$$\begin{aligned} & \left(2(24a^3Cd^2f - a^2bd(23Cde + 41cCf + 4Bdf)) - b^3(15c^2Ce - 2Ad^2e + cd(5Be + Af)) + \right. \\ & \quad \left. ab^2(15c^2Cf + d^2(3Be - Af) + c(40Cde + 6Bdf)) \right) \sqrt{c+dx} \sqrt{e+fx} / \\ & \left(15b^3(bc-ad)^2(be-af)\sqrt{a+bx} \right) + \left(2(6a^3Cdf + ab^2(10cCe + 3Bde + 3Bcf - 4Adf)) - \right. \\ & \quad \left. b^3(5Bce - 2A(de+cf)) - a^2b(Bdf + 8C(de+cf)) \right) \sqrt{c+dx} (e+fx)^{3/2} / \\ & \left(15b^2(bc-ad)(be-af)^2(a+bx)^{3/2} \right) - \frac{2(Ab^2 - a(bB - aC))(c+dx)^{3/2}(e+fx)^{3/2}}{5b(bc-ad)(be-af)(a+bx)^{5/2}} + \end{aligned}$$

1

$$15b^4(-bc+ad)^{3/2}(be-af)^2\sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}$$

$$\begin{aligned} & 2\sqrt{d}(48a^4Cd^2f^2 - 8a^3bdf(Bdf + 11C(de+cf)) - \\ & \quad b^4(2Ad^2e^2 - cde(5Be + 2Af) - c^2(30Ce^2 + 5Bef - 2Af^2)) - \\ & \quad ab^3(d^2e(3Be - 2Af) + c^2f(70Ce + 3Bf) + 2cd(35Ce^2 + 11Bef - Af^2)) + \\ & \quad a^2b^2(2C(19d^2e^2 + 81cdef + 19c^2f^2) - df(2Adf - 13B(de+cf)))) \end{aligned}$$

$$\sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] +$$

$$\begin{aligned} & \left(2(de - cf)(24a^3Cd^2f - a^2bd(23Cde + 41cCf + 4Bdf)) - b^3 \right. \\ & \quad \left. (15c^2Ce - 2Ad^2e + cd(5Be + Af)) + ab^2(15c^2Cf + d^2(3Be - Af) + c(40Cde + 6Bdf)) \right) \\ & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] / \\ & \left(15b^4\sqrt{d}(-bc+ad)^{3/2}(be-af)\sqrt{c+dx}\sqrt{e+fx} \right) \end{aligned}$$

Result (type 4, 9529 leaves):

$$\begin{aligned} & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\ & \left(-\frac{2(Ab^2 - abB + a^2C)}{5b^3(a+bx)^3} - (2(5b^3Bce - 10ab^2cCe + Ab^3de - 6ab^2Bde + 11a^2bCde + \right. \end{aligned}$$

$$\begin{aligned}
 & \left(A b^3 c f - 6 a b^2 B c f + 11 a^2 b c C f - 2 a A b^2 d f + 7 a^2 b B d f - 12 a^3 C d f \right) / \\
 & \left(15 b^3 (b c - a d) (b e - a f) (a + b x)^2 \right) - \frac{1}{15 b^3 (b c - a d)^2 (b e - a f)^2 (a + b x)} \\
 & 2 \left(15 b^4 c^2 C e^2 + 5 b^4 B c d e^2 - 40 a b^3 c C d e^2 - 2 A b^4 d^2 e^2 - 3 a b^3 B d^2 e^2 + 23 a^2 b^2 C d^2 e^2 + \right. \\
 & \quad 5 b^4 B c^2 e f - 40 a b^3 c^2 C e f + 2 A b^4 c d e f - 22 a b^3 B c d e f + 102 a^2 b^2 c C d e f + \\
 & \quad 2 a A b^3 d^2 e f + 13 a^2 b^2 B d^2 e f - 58 a^3 b c C d^2 e f - 2 A b^4 c^2 f^2 - 3 a b^3 B c^2 f^2 + 23 a^2 b^2 c^2 C f^2 + 2 \\
 & \quad \left. a A b^3 c d f^2 + 13 a^2 b^2 B c d f^2 - 58 a^3 b c C d f^2 - 2 a^2 A b^2 d^2 f^2 - 8 a^3 b B d^2 f^2 + 33 a^4 C d^2 f^2 \right) + \\
 & \frac{1}{15 b^5 (b c - a d)^2 (b e - a f)^2} 2 \left(\frac{1}{\sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}} \right. \\
 & \quad \left(30 b^4 c^2 C e^2 + 5 b^4 B c d e^2 - 70 a b^3 c C d e^2 - 2 A b^4 d^2 e^2 - 3 a b^3 B d^2 e^2 + 38 a^2 b^2 C d^2 e^2 + \right. \\
 & \quad 5 b^4 B c^2 e f - 70 a b^3 c^2 C e f + 2 A b^4 c d e f - 22 a b^3 B c d e f + 162 a^2 b^2 c C d e f + \\
 & \quad 2 a A b^3 d^2 e f + 13 a^2 b^2 B d^2 e f - 88 a^3 b c C d^2 e f - 2 A b^4 c^2 f^2 - 3 a b^3 B c^2 f^2 + 38 a^2 b^2 c^2 C f^2 + \\
 & \quad \left. 2 a A b^3 c d f^2 + 13 a^2 b^2 B c d f^2 - 88 a^3 b c C d f^2 - 2 a^2 A b^2 d^2 f^2 - 8 a^3 b B d^2 f^2 + 48 a^4 C d^2 f^2 \right) \\
 & \quad (a + b x)^{3/2} \left(d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \left(f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right) - \\
 & \frac{1}{\sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}} (b c - a d) (b e - a f) (a + b x) \\
 & \sqrt{\left(d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \left(f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right)} \\
 & \left(\left(30 i b^4 c^2 C e^2 f \sqrt{1 - \frac{-b c + a d}{d (a + b x)}} \sqrt{1 - \frac{-b e + a f}{f (a + b x)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-b c + a d}{d}}}{\sqrt{a + b x}} \right] \right), \right. \right. \right. \\
 & \quad \left. \left. \frac{d (-b e + a f)}{(-b c + a d) f} \right) - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-b c + a d}{d}}}{\sqrt{a + b x}} \right], \frac{d (-b e + a f)}{(-b c + a d) f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-b c + a d}{d}} (-b e + a f) \sqrt{\left(d + \frac{b c - a d}{a + b x} \right) \left(f + \frac{b e - a f}{a + b x} \right)} \right) +
 \end{aligned}$$

$$\left(5 i b^4 B c d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(70 i a b^3 c \right)$$

$$C d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i A b^4 d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i a b^3 B d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(38 i a^2 b^2 C \right)$$

$$d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5 i b^4 B c^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(70 i a b^3 c^2 \right)$$

$$\begin{aligned}
 & c e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(2 i A b^4 c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(22 i a b^3 B \right. \\
 & \left. c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\left(162 i a^2 b^2 c C d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(2 i a A b^3 d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(13 i a^2 b^2 B d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(88 \text{i} a^3 b c d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) - \right. \\
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 \text{i} A b^4 c^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(3 \, i \, a \, b^3 \, B \, c^2 \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(38 \, i \, a^2 \, b^2 \, c^2 \, C \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(2 \, i \, a \, A \, b^3 \, c \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(13 i a^2 b^2 B c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(88 i a^3 b c C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i a^2 A b^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i a^3 b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(48 i a^4 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(15 i b^3 c C d e^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i a b^2 c d^2 e^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(15 i b^3 c^2 C e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(10 i b^3 B c d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(80 i a b^2 c C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(i A b^3 d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right.$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(9 i a b^2 B d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right.$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(64 i a^2 b C d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right.$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(15 i a b^2 c^2 C f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \right.$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(i A b^3 c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(9 i a b^2 B c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(64 i a^2 b c C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(2 i a A b^2 d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /
 \end{aligned}$$

$$\left(\sqrt{-\frac{bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(8i a^2 b B d^2 f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\ \left(\sqrt{-\frac{bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(48i a^3 C d^2 f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\ \left(\sqrt{-\frac{bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 66: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} \sqrt{e+fx} (A+Bx+Cx^2)}{(a+bx)^{9/2}} dx$$

Optimal (type 4, 1716 leaves, 10 steps):

$$\begin{aligned}
 & - \left(\left(2 \left(24 a^4 C d^2 f^2 - a^3 b d f (61 C d e + 43 c C f - 4 B d f) - \right. \right. \right. \\
 & \quad \left. \left. \left. 3 a b^3 (d^2 e (B e - 3 A f) + 2 c^2 f (7 C e - B f) + c d (28 C e^2 - 5 B e f + 5 A f^2)) - \right. \right. \right. \\
 & \quad \left. \left. \left. b^4 (4 A d^2 e^2 - c d e (7 B e - A f) - c^2 (35 C e^2 - 14 B e f + 8 A f^2)) - \right. \right. \right. \\
 & \quad \left. \left. \left. 3 a^2 b^2 (d f (3 B d e + 2 B c f - A d f) - C (15 d^2 e^2 + 37 c d e f + 5 c^2 f^2)) \right) \sqrt{c+dx} \sqrt{e+fx} \right) / \\
 & \quad \left(105 b^3 (bc-ad)^2 (be-af)^2 (a+bx)^{3/2} \right) + \frac{1}{105 b^3 (bc-ad)^3 (be-af)^3 \sqrt{a+bx}} \\
 & 2 \left(48 a^5 C d^3 f^3 + 8 a^4 b d^2 f^2 (B d f - 16 C (de+cf)) - \right. \\
 & \quad b^5 (8 A d^3 e^3 - c d^2 e^2 (14 B e + 5 A f) + c^2 d e (35 C e^2 + 14 B e f - 5 A f^2) + \\
 & \quad \left. c^3 f (35 C e^2 - 14 B e f + 8 A f^2)) - a b^4 (d^3 e^2 (6 B e - 19 A f) - 6 c^3 f^2 (7 C e - B f) - \right. \\
 & \quad \left. c^2 d f (238 C e^2 - 19 f (B e - A f)) - c d^2 e (42 C e^2 - f (19 B e + 20 A f))) \right) + \\
 & \quad a^3 b^2 d f (C (103 d^2 e^2 + 344 c d e f + 103 c^2 f^2) + d f (6 A d f - 19 B (de+cf))) - \\
 & \quad \left. 3 a^2 b^3 (C (5 d^3 e^3 + 94 c d^2 e^2 f + 94 c^2 d e f^2 + 5 c^3 f^3) + \right. \\
 & \quad \left. d f (3 A d f (de+cf) - B (3 d^2 e^2 + 16 c d e f + 3 c^2 f^2))) \right) \sqrt{c+dx} \sqrt{e+fx} + \\
 & \left(2 (6 a^3 C d f + a b^2 (14 c C e + 3 B d e + 3 B c f - 8 A d f) - b^3 (7 B c e - 4 A (de+cf))) + \right. \\
 & \quad \left. a^2 b (B d f - 10 C (de+cf)) \right) \sqrt{c+dx} (e+fx)^{3/2} / \\
 & \left(35 b^2 (bc-ad) (be-af)^2 (a+bx)^{5/2} \right) - \\
 & \frac{2 (A b^2 - a (b B - a C)) (c+dx)^{3/2} (e+fx)^{3/2}}{7 b (bc-ad) (be-af) (a+bx)^{7/2}} + \\
 & \frac{1}{105 b^4 (-bc+ad)^{5/2} (be-af)^3 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}} \\
 & 2 \sqrt{d} \left(48 a^5 C d^3 f^3 + 8 a^4 b d^2 f^2 (B d f - 16 C (de+cf)) - \right. \\
 & \quad b^5 (8 A d^3 e^3 - c d^2 e^2 (14 B e + 5 A f) + c^2 d e (35 C e^2 + 14 B e f - 5 A f^2) + \\
 & \quad \left. c^3 f (35 C e^2 - 14 B e f + 8 A f^2)) - a b^4 (d^3 e^2 (6 B e - 19 A f) - 6 c^3 f^2 (7 C e - B f) - \right. \\
 & \quad \left. c^2 d f (238 C e^2 - 19 f (B e - A f)) - c d^2 e (42 C e^2 - f (19 B e + 20 A f))) \right) + \\
 & \quad a^3 b^2 d f (C (103 d^2 e^2 + 344 c d e f + 103 c^2 f^2) + d f (6 A d f - 19 B (de+cf))) - \\
 & \quad \left. 3 a^2 b^3 (C (5 d^3 e^3 + 94 c d^2 e^2 f + 94 c^2 d e f^2 + 5 c^3 f^3) + \right. \\
 & \quad \left. d f (3 A d f (de+cf) - B (3 d^2 e^2 + 16 c d e f + 3 c^2 f^2))) \right) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] + \\
 & \frac{1}{105 b^4 (-bc+ad)^{5/2} (be-af)^2 \sqrt{c+dx} \sqrt{e+fx}} \\
 & 2 \sqrt{d} (de-cf) \\
 & \left(24 a^4 C d^2 f^2 - a^3 b d f (43 C d e + 61 c C f - 4 B d f) + \right. \\
 & \quad b^4 (8 A d^2 e^2 - c d e (14 B e + A f) + c^2 (35 C e^2 + 7 B e f - 4 A f^2)) + \\
 & \quad \left. 3 a b^3 (d^2 e (2 B e - 5 A f) - c^2 f (28 C e + B f) - c d (14 C e^2 - 5 B e f - 3 A f^2)) - \right. \\
 & \quad \left. 3 a^2 b^2 (d f (2 B d e + 3 B c f - A d f) - C (5 d^2 e^2 + 37 c d e f + 15 c^2 f^2)) \right) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right]
 \end{aligned}$$

Result (type 4, 15719 leaves):

$$\begin{aligned} & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\ & \left(-\frac{2(Ab^2 - abB + a^2C)}{7b^3(a+bx)^4} - (2(7b^3Bce - 14ab^2cCe + Ab^3de - 8ab^2Bde + 15a^2bcde + \right. \\ & \quad \left. Ab^3cf - 8ab^2Bcf + 15a^2bccf - 2aAb^2df + 9a^2bBdf - 16a^3cdf)) / \right. \\ & \quad \left. (35b^3(bc-ad)(be-af)(a+bx)^3) - \frac{1}{105b^3(bc-ad)^2(be-af)^2(a+bx)^2} \right. \\ & \quad \left. 2(35b^4c^2Ce^2 + 7b^4Bcde^2 - 84ab^3cCde^2 - 4Ab^4d^2e^2 - 3ab^3Bd^2e^2 + 45a^2b^2Cd^2e^2 + 7b^4B \right. \\ & \quad \left. c^2ef - 84ab^3c^2Cef + 2Ab^4cdef - 30ab^3Bcdef + 198a^2b^2cCdef + 6aAb^3d^2ef + \right. \\ & \quad \left. 15a^2b^2Bd^2ef - 106a^3bc d^2ef - 4Ab^4c^2f^2 - 3ab^3Bc^2f^2 + 45a^2b^2c^2Cf^2 + 6aAb^3cd^2f^2 + \right. \\ & \quad \left. 15a^2b^2Bcd^2f^2 - 106a^3bccd^2f^2 - 6a^2Ab^2d^2f^2 - 8a^3bBd^2f^2 + 57a^4Cd^2f^2) - \right. \\ & \quad \left. \frac{1}{105b^3(bc-ad)^3(be-af)^3(a+bx)} 2(35b^5c^2Cde^3 - 14b^5Bcd^2e^3 - 42ab^4cCd^2e^3 + \right. \\ & \quad \left. 8Ab^5d^3e^3 + 6ab^4Bd^3e^3 + 15a^2b^3Cd^3e^3 + 35b^5c^3Ce^2f + 14b^5Bc^2d^2ef - \right. \\ & \quad \left. 238ab^4c^2Cde^2f - 5Ab^5cd^2e^2f + 19ab^4Bcd^2e^2f + 282a^2b^3cCd^2e^2f - 19aAb^4d^3e^2f - \right. \\ & \quad \left. 9a^2b^3Bd^3e^2f - 103a^3b^2Cd^3e^2f - 14b^5Bc^3ef^2 - 42ab^4c^3Cef^2 - 5Ab^5c^2def^2 + \right. \\ & \quad \left. 19ab^4Bc^2def^2 + 282a^2b^3c^2Cdef^2 + 20aAb^4cd^2ef^2 - 48a^2b^3Bcd^2ef^2 - 344a^3b^2cC \right. \\ & \quad \left. d^2ef^2 + 9a^2Ab^3d^3ef^2 + 19a^3b^2Bd^3ef^2 + 128a^4bc d^3ef^2 + 8Ab^5c^3f^3 + 6ab^4Bc^3f^3 + \right. \\ & \quad \left. 15a^2b^3c^3Cf^3 - 19aAb^4c^2df^3 - 9a^2b^3Bc^2df^3 - 103a^3b^2c^2Cdf^3 + 9a^2Ab^3cd^2f^3 + \right. \\ & \quad \left. 19a^3b^2Bcd^2f^3 + 128a^4bccd^2f^3 - 6a^3Ab^2d^3f^3 - 8a^4bBd^3f^3 - 48a^5Cd^3f^3) \right) - \\ & \frac{1}{105b^5(bc-ad)^3(be-af)^3} 2df \left(\frac{1}{df \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right. \\ & \quad \left. (-35b^5c^2Cde^3 + 14b^5Bcd^2e^3 + 42ab^4cCd^2e^3 - 8Ab^5d^3e^3 - 6ab^4Bd^3e^3 - \right. \\ & \quad \left. 15a^2b^3Cd^3e^3 - 35b^5c^3Ce^2f - 14b^5Bc^2d^2ef + 238ab^4c^2Cde^2f + 5Ab^5cd^2e^2f - \right. \\ & \quad \left. 19ab^4Bcd^2e^2f - 282a^2b^3cCd^2e^2f + 19aAb^4d^3e^2f + 9a^2b^3Bd^3e^2f + \right. \\ & \quad \left. 103a^3b^2Cd^3e^2f + 14b^5Bc^3ef^2 + 42ab^4c^3Cef^2 + 5Ab^5c^2def^2 - 19ab^4Bc^2def^2 - \right. \\ & \quad \left. 282a^2b^3c^2Cdef^2 - 20aAb^4cd^2ef^2 + 48a^2b^3Bcd^2ef^2 + 344a^3b^2cCd^2ef^2 - \right. \\ & \quad \left. 9a^2Ab^3d^3ef^2 - 19a^3b^2Bd^3ef^2 - 128a^4bc d^3ef^2 - 8Ab^5c^3f^3 - 6ab^4Bc^3f^3 - \right. \\ & \quad \left. 15a^2b^3c^3Cf^3 + 19aAb^4c^2df^3 + 9a^2b^3Bc^2df^3 + 103a^3b^2c^2Cdf^3 - 9a^2Ab^3cd^2f^3 - \right. \\ & \quad \left. 19a^3b^2Bcd^2f^3 - 128a^4bccd^2f^3 + 6a^3Ab^2d^3f^3 + 8a^4bBd^3f^3 + 48a^5Cd^3f^3) \right. \\ & \quad \left. (a+bx)^{3/2} \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) + \right. \\ & \quad \left. \frac{1}{df \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} (-bc+ad)(-be+af) \right. \\ & \quad \left. (a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \right) \end{aligned}$$

$$\left(\left(35 \, i \, b^5 \, c^2 \, C \, d \, e^3 \, f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\ \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(14 \, i \, b^5 \, B \, c \right.$$

$$d^2 \, e^3 \, f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(42 \, i \, a \, b^4 \, c \, C \right.$$

$$d^2 \, e^3 \, f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i A b^5 d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a b^4 B d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i a^2 b^3 C \right)$$

$$d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right], \right)$$

$$\left(\frac{d(-be+af)}{(-bc+ad)f} \right) - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(35 \, i \, b^5 \, c^3 \, C \, e^2 \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(14 \, i \, b^5 \, B \, c^2$$

$$d \, e^2 \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(238 \, i \, a \, b^4 \, c^2$$

$$C \, d \, e^2 \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(5 i A b^5 c d^2 \right.$$

$$e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(19 i a b^4 B c \right.$$

$$d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(282 i a^2 b^3 c \right.$$

$$C d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(19 i a A b^4$$

$$d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right],$$

$$\frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(9 i a^2 b^3 B$$

$$d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right],$$

$$\frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(103 i a^3 b^2 C d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(14 i b^5 B c^3 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(42 i a b^4 c^3 C e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(5 \, i \, A b^5 c^2 d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \quad \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(19 \, i \, a b^4 B c^2 d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \quad \left. \left(\text{EllipticE}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \\
 & \quad \left. \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(282 \, i \, a^2 b^3 c^2 C d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.
 \end{aligned}$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \\
 \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 \left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 \left(20 i a A b^4 c d^2 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) \\
 \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \\
 \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 \left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 \left(48 i a^2 b^3 B c d^2 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right) \\
 \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(344 i a^3 b^2 c C d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) -$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(9 i a^2 A b^3 d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) -$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(19 i a^3 b^2 B d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(128 i a^4 b C d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\left(8 i A b^5 c^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a b^4 B c^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(15 i a^2 b^3 c^3 C f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(19 i a A b^4 c^2 d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(9 i a^2 b^3 B c^2 d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(103 i a^3 b^2 c^2 C d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(9 i a^2 A b^3 c d^2 f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(19 i a^3 b^2 B c d^2 f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(128 \text{i} a^4 b c C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) - \right. \\
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(6 \text{i} a^3 A b^2 d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] \right) - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(8 i a^4 b B d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(48 i a^5 C d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(70 i b^4 c^2 C d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(7 i b^4 B c d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right),$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(126 i a b^3 c C d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(4 i A b^4 d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(3 i a b^3 B d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(60 i a^2 b^2 C d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\begin{aligned}
 & \left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(7i b^4 B c^2 d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(126i a b^3 c^2 C d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(2i A b^4 c d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\
 & \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(30i a b^3 B c d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.
 \end{aligned}$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(222 i a^2 b^2 c C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(6 i a A b^3 d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(15 i a^2 b^2 B d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(104 \, i \, a^3 \, b \, C \, d^3 \, e \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(4 \, i \, A \, b^4 \, c^2 \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(3 \, i \, a \, b^3 \, B \, c^2 \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(60 \, i \, a^2 \, b^2 \, c^2 \, C \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \, \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(6 \, i \, a \, A \, b^3 \, c \, d^2 \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 \, i \, a^2 \, b^2 \, B \, c \, d^2 \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(104 \, i \, a^3 \, b \, c \, C \, d^2 \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(6 \, i \, a^2 \, A \, b^2 \, d^3 \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8i a^3 b B d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(48i a^4 C d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 67: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a+bx)^{3/2} \sqrt{c+dx} (A+Bx+Cx^2)}{\sqrt{e+fx}} dx$$

Optimal (type 4, 1235 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{1}{945 b^2 d^3 f^4} 2 \left(5 b d f (7 a d f (5 b c C e + 3 a C d e + a c C f - 9 A b d f) - \right. \\
 & \quad \left. (3 b c e + 3 a d e + a c f) (4 a C d f + b (8 C d e + 6 c C f - 9 B d f)) \right) + \\
 & \quad 2 \left(\frac{a d f}{2} - b (2 d e + c f) \right) (7 b d f (5 b c C e + 3 a C d e + a c C f - 9 A b d f) - \\
 & \quad \left. (6 b d e + 4 b c f - 3 a d f) (4 a C d f + b (8 C d e + 6 c C f - 9 B d f)) \right) \sqrt{a + b x} \\
 & \quad \sqrt{c + d x} \sqrt{e + f x} - \frac{1}{315 b d^3 f^3} 2 (7 b d f (5 b c C e + 3 a C d e + a c C f - 9 A b d f) - \\
 & \quad (6 b d e + 4 b c f - 3 a d f) (4 a C d f + b (8 C d e + 6 c C f - 9 B d f))) \\
 & \quad \sqrt{a + b x} (c + d x)^{3/2} \sqrt{e + f x} - \frac{1}{63 b d^2 f^2} \\
 & 2 (4 a C d f + b (8 C d e + 6 c C f - 9 B d f)) \\
 & \quad (a + b x)^{3/2} \\
 & \quad (c + d x)^{3/2} \\
 & \quad \sqrt{e + f x} + \\
 & \frac{2 C (a + b x)^{5/2} (c + d x)^{3/2} \sqrt{e + f x}}{9 b d f} + \\
 & \frac{1}{315 b^3 d^{7/2} f^5 \sqrt{c + d x} \sqrt{\frac{b(e+fx)}{be-af}}} \\
 & 2 \sqrt{-bc+ad} (8 a^4 C d^4 f^4 + a^3 b d^3 f^3 (11 C d e - 7 c C f - 18 B d f) - \\
 & \quad 3 a^2 b^2 d^2 f^2 (3 d f (4 B d e - 3 B c f - 7 A d f) - C (9 d^2 e^2 - 5 c d e f - 3 c^2 f^2)) - \\
 & \quad a b^3 d f (2 C (92 d^3 e^3 - 33 c d^2 e^2 f - 18 c^2 d e f^2 - 16 c^3 f^3) + \\
 & \quad 3 d f (7 A d f (13 d e - 7 c f) - B (72 d^2 e^2 - 29 c d e f - 19 c^2 f^2))) + \\
 & \quad b^4 (C (128 d^4 e^4 - 40 c d^3 e^3 f - 21 c^2 d^2 e^2 f^2 - 16 c^3 d e f^3 - 16 c^4 f^4) + \\
 & \quad 3 d f (7 A d f (8 d^2 e^2 - 3 c d e f - 2 c^2 f^2) - B (48 d^3 e^3 - 16 c d^2 e^2 f - 9 c^2 d e f^2 - 8 c^3 f^3)))) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] + \\
 & \frac{1}{315 b^3 d^{7/2} f^5 \sqrt{c+dx} \sqrt{e+fx}} 2 \sqrt{-bc+ad} (be-af) (de-cf) \\
 & \quad (4 a^3 C d^3 f^3 + 3 a^2 b d^2 f^2 (3 C d e - c C f - 3 B d f) - \\
 & \quad 3 a b^2 d f (3 d f (16 B d e + 3 B c f - 21 A d f) - 5 C (8 d^2 e^2 + 2 c d e f + c^2 f^2)) - \\
 & \quad b^3 (C (128 d^3 e^3 + 24 c d^2 e^2 f + 15 c^2 d e f^2 + 8 c^3 f^3) + \\
 & \quad 3 d f (7 A d f (8 d e + c f) - 4 B (12 d^2 e^2 + 2 c d e f + c^2 f^2)))) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right]
 \end{aligned}$$

Result (type 4, 12483 leaves):

$$\begin{aligned}
 & \sqrt{a + b x} \sqrt{c + d x} \sqrt{e + f x} \\
 & \left(- \frac{1}{315 b^2 d^3 f^4} 2 (64 b^3 C d^3 e^3 - 12 b^3 c C d^2 e^2 f - 72 b^3 B d^3 e^2 f - 84 a b^2 C d^3 e^2 f - \right. \\
 & \quad \left. 9 b^3 c^2 C d e f^2 + 15 b^3 B c d^2 e f^2 + 19 a b^2 c C d^2 e f^2 + 84 A b^3 d^3 e f^2 + 99 a b^2 B d^3 e f^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 a^2 b c d^3 e f^2 - 8 b^3 c^3 C f^3 + 12 b^3 B c^2 d f^3 + 15 a b^2 c^2 C d f^3 - 21 A b^3 c d^2 f^3 - \\
 & 27 a b^2 B c d^2 f^3 - 3 a^2 b c C d^2 f^3 - 126 a A b^2 d^3 f^3 - 9 a^2 b B d^3 f^3 + 4 a^3 C d^3 f^3) + \\
 & \frac{1}{315 b d^2 f^3} 2 (48 b^2 C d^2 e^2 - 7 b^2 c C d e f - 54 b^2 B d^2 e f - 61 a b C d^2 e f - 6 b^2 c^2 C f^2 + \\
 & 9 b^2 B c d f^2 + 11 a b c C d f^2 + 63 A b^2 d^2 f^2 + 72 a b B d^2 f^2 + 3 a^2 C d^2 f^2) x + \\
 & 2 \left(\frac{-8 b C d e + b c C f + 9 b B d f + 10 a C d f}{63 d f^2} x^2 + \frac{2 b C x^3}{9 f} \right) + \\
 & \frac{1}{315 b^4 d^3 f^4} 2 \left(\frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right. \\
 & (128 b^4 C d^4 e^4 - 40 b^4 c C d^3 e^3 f - 144 b^4 B d^4 e^3 f - 184 a b^3 C d^4 e^3 f - 21 b^4 c^2 C d^2 e^2 f^2 + \\
 & 48 b^4 B c d^3 e^2 f^2 + 66 a b^3 c C d^3 e^2 f^2 + 168 A b^4 d^4 e^2 f^2 + 216 a b^3 B d^4 e^2 f^2 + \\
 & 27 a^2 b^2 C d^4 e^2 f^2 - 16 b^4 c^3 C d e f^3 + 27 b^4 B c^2 d^2 e f^3 + 36 a b^3 c^2 C d^2 e f^3 - 63 A b^4 c d^3 e f^3 - \\
 & 87 a b^3 B c d^3 e f^3 - 15 a^2 b^2 c C d^3 e f^3 - 273 a A b^3 d^4 e f^3 - 36 a^2 b^2 B d^4 e f^3 + 11 a^3 b C d^4 e f^3 - \\
 & 16 b^4 c^4 C f^4 + 24 b^4 B c^3 d f^4 + 32 a b^3 c^3 C d f^4 - 42 A b^4 c^2 d^2 f^4 - 57 a b^3 B c^2 d^2 f^4 - \\
 & 9 a^2 b^2 c^2 C d^2 f^4 + 147 a A b^3 c d^3 f^4 + 27 a^2 b^2 B c d^3 f^4 - 7 a^3 b c C d^3 f^4 + 63 a^2 A b^2 d^4 f^4 - \\
 & 18 a^3 b B d^4 f^4 + 8 a^4 C d^4 f^4) (a+bx)^{3/2} \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) - \\
 & \frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} (-bc+ad) (-be+af) (a+bx) \\
 & \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \\
 & \left(\left(128 i b^4 C d^4 e^4 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} - 40 i b^4 c C \right.
 \end{aligned}$$

$$\begin{aligned}
 & d^3 e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(144 i b^4 B \right. \\
 & d^4 e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(184 i a b^3 C \right. \\
 & d^4 e^3 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(21 i b^4 c^2 C \right. \\
 & d^2 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(48 i b^4 B c \right. \\
 & d^3 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(66 i a b^3 c C \right. \\
 & d^3 e^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(168 i A b^4 \right.$$

$$d^4 e^2 f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(216 i a b^3 B \right.$$

$$d^4 e^2 f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(27 i a^2 b^2 C d^4 e^2 f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(16 i b^4 c^3 C d e f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(27 i b^4 B c^2 d^2 e f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(36 i a b^3 c^2 C d^2 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right) \\
 & \left(\left. \left. \left. \text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) - \right. \\
 & \left. \left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(63 i A b^4 c d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right) \\
 & \left(\left. \left. \left. \text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) - \right. \\
 & \left. \left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /
 \end{aligned}$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(87 i a b^3 B c d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(15 i a^2 b^2 c C d^3 e f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(273 \, i \, a \, A \, b^3 \, d^4 \, e \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(36 \, i \, a^2 \, b^2 \, B \, d^4 \, e \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(11 \, i \, a^3 \, b \, C \, d^4 \, e \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(16 i b^4 c^4 C f^5 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(24 i b^4 B c^3 d f^5 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(32 i a b^3 c^3 C d f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(42 i A b^4 c^2 d^2 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(57 i a b^3 B c^2 d^2 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(9 i a^2 b^2 c^2 d^2 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) -$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(147 i a A b^3 c d^3 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) -$$

$$\left(\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(27 i a^2 b^2 B c d^3 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(7 i a^3 b c C d^3 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(63 i a^2 A b^2 d^4 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(18 \text{i} a^3 b B d^4 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 \text{i} a^4 C d^4 f^5 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(64 \text{i} b^3 C d^4 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(12 i b^3 c C d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(72 i b^3 B d^4 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(36 i a b^2 C d^4 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(9 i b^3 c^2 C d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left. \sqrt{1 - \frac{-bc+ad}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-bc+af)}{(-bc+ad)f}\right]\right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(15 i b^3 B c d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-bc+ad}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-bc+af)}{(-bc+ad)f}\right]\right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(12 i a b^2 c C d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-bc+ad}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-bc+af)}{(-bc+ad)f}\right]\right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(84 i A b^3 d^4 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left. \left. \sqrt{1 - \frac{-bc+ad}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}}\right], \frac{d(-bc+af)}{(-bc+ad)f}\right]\right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(45 i a b^2 B d^4 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right.$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(15 i a^2 b c d^4 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(8 i b^3 c^3 c d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(12 i b^3 B c^2 d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(9 i a b^2 c^2 C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(21 i A b^3 c d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(18 i a b^2 B c d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(3 i a^2 b c C d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(63 i a A b^2 d^4 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(18 i a^2 b B d^4 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i a^3 C d^4 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 68: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+bx} \sqrt{c+dx} (A+Bx+Cx^2)}{\sqrt{e+fx}} dx$$

Optimal (type 4, 766 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{105 b^2 d^2 f^3} 2 (5 b d f (3 b c C e + 3 a C d e + a c C f - 7 A b d f) + \\
 & \quad (a d f - 2 b (2 d e + c f)) (4 a C d f + b (6 C d e + 4 c C f - 7 B d f))) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} - \\
 & \frac{1}{35 b d^2 f^2} 2 (4 a C d f + b (6 C d e + 4 c C f - 7 B d f)) \sqrt{a+bx} (c+dx)^{3/2} \sqrt{e+fx} + \\
 & \frac{2 C (a+bx)^{3/2} (c+dx)^{3/2} \sqrt{e+fx}}{7 b d f} - \frac{1}{105 b^3 d^{5/2} f^4 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}} \\
 & 2 \sqrt{-bc+ad} \left(3 b d f (5 a d f (3 b c C e + 3 a C d e + a c C f - 7 A b d f) - \right. \\
 & \quad (b c e + 3 a d e + a c f) (4 a C d f + b (6 C d e + 4 c C f - 7 B d f))) + \\
 & \quad \left. 2 \left(\frac{b c f}{2} - d (b e + a f) \right) (5 b d f (3 b c C e + 3 a C d e + a c C f - 7 A b d f) + \right. \\
 & \quad \left. (a d f - 2 b (2 d e + c f)) (4 a C d f + b (6 C d e + 4 c C f - 7 B d f))) \right) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] + \\
 & \left(2 \sqrt{-bc+ad} (be-af) (de-cf) (4 a^2 C d^2 f^2 + a b d f (8 C d e - 2 c C f - 7 B d f) - \right. \\
 & \quad \left. b^2 (7 d f (8 B d e + B c f - 10 A d f) - 4 C (12 d^2 e^2 + 2 c d e f + c^2 f^2))) \right) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] \Big/ \\
 & (105 b^3 d^{5/2} f^4 \sqrt{c+dx} \sqrt{e+fx})
 \end{aligned}$$

Result (type 4, 7297 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\
 & \left(\frac{1}{105 b^2 d^2 f^3} 2 (24 b^2 C d^2 e^2 - 5 b^2 c C d e f - 28 b^2 B d^2 e f - 5 a b C d^2 e f - 4 b^2 c^2 C f^2 + \right. \\
 & \quad \left. 7 b^2 B c d f^2 + 2 a b c C d f^2 + 35 A b^2 d^2 f^2 + 7 a b B d^2 f^2 - 4 a^2 C d^2 f^2) + \right. \\
 & \quad \left. \frac{2 (-6 b C d e + b c C f + 7 b B d f + a C d f) x}{35 b d f^2} + \frac{2 C x^2}{7 f} \right) + \frac{1}{105 b^4 d^2 f^3} \\
 & 2 \left(\frac{1}{d f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} (-48 b^3 C d^3 e^3 + 16 b^3 c C d^2 e^2 f + 56 b^3 B d^3 e^2 f + \right. \\
 & \quad \left. 16 a b^2 C d^3 e^2 f + 9 b^3 c^2 C d e f^2 - 21 b^3 B c d^2 e f^2 - 8 a b^2 c C d^2 e f^2 - 70 A b^3 d^3 e f^2 - \right. \\
 & \quad \left. 21 a b^2 B d^3 e f^2 + 9 a^2 b C d^3 e f^2 + 8 b^3 c^3 C f^3 - 14 b^3 B c^2 d f^3 - 5 a b^2 c^2 C d f^3 + 35 A b^3 c d^2 f^3 + \right. \\
 & \quad \left. 14 a b^2 B c d^2 f^3 - 5 a^2 b c C d^2 f^3 + 35 a A b^2 d^3 f^3 - 14 a^2 b B d^3 f^3 + 8 a^3 C d^3 f^3) (a+bx)^{3/2} \right)
 \end{aligned}$$

$$\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) + \frac{1}{df \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}}$$

$$(-bc+ad)(-be+af)(a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)}$$

$$\left(\left(48 i b^3 C d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(16 i b^3 c c \right.$$

$$d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(56 i b^3 B d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(16 \text{i} a b^2 C \right.$$

$$d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(9 \text{i} b^3 c^2 C d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(21 \text{i} b^3 B c \right.$$

$$d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(8 \text{i} a b^2 c c \right.$$

$$d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(70 \text{i} A b^3 d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(21 \text{i} a b^2 B d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(9 i a^2 b c d^3 e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i b^3 c^3 c f^4 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(14 \, i \, b^3 \, B \, c^2 \, d \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5 \, i \, a \, b^2 \, c^2 \, C \, d \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(35 \, i \, A \, b^3 \, c \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(14 i a b^2 B c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5 i a^2 b c C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(35 i a A b^2 d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(14 \, i \, a^2 b B d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(8 \, i \, a^3 C d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(24 \, i \, b^2 C d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(5 \, i \, b^2 \, c \, C \, d^2 \, e \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\
 & \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(28 \, i \, b^2 \, B \, d^3 \, e \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\
 & \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(13 \, i \, a \, b \, C \, d^3 \, e \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\
 & \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(4 \, i \, b^2 \, c^2 \, C \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \\
 & \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /
 \end{aligned}$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(7 i b^2 B c d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(i a b c C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(35 i A b^2 d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(14 i a b B d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left(8 i a^2 C d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) / \left(\sqrt{\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right)$$

Problem 69: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} (A+Bx+Cx^2)}{\sqrt{a+bx} \sqrt{e+fx}} dx$$

Optimal (type 4, 527 leaves, 8 steps):

$$\begin{aligned} & - \frac{2(4aCdf + b(4Cde + 2cCf - 5Bdf)) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx}}{15b^2d^2} + \\ & \frac{2C\sqrt{a+bx} (c+dx)^{3/2} \sqrt{e+fx}}{5bdf} - \left(2\sqrt{-bc+ad} (3bdf(bcCe + 3aCde + acCf - 5Abdf) - \right. \\ & \quad \left. (2bde - bcf + 2adf)(4aCdf + b(4Cde + 2cCf - 5Bdf))) \right) \\ & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \Big/ \\ & \left(15b^3d^{3/2}f^3\sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}} - \left(2\sqrt{-bc+ad} (de - cf) \right. \right. \\ & \quad \left. \left. (4a^2Cdf^2 + abf(3Cde - cCf - 5Bdf) - b^2(5df(2Be - 3Af) - Ce(8de + cf))) \right) \right) \\ & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \Big/ \\ & (15b^3d^{3/2}f^3\sqrt{c+dx} \sqrt{e+fx}) \end{aligned}$$

Result (type 4, 5393 leaves):

$$\sqrt{a+bx} \sqrt{c+dx} \left(\frac{2(-4bcde + bccf + 5bBdf - 4aCdf)}{15b^2d^2} + \frac{2Cx}{5bf} \right) \sqrt{e+fx} +$$

$$\begin{aligned}
 & \frac{1}{15 b^4 d f^2} 2 \left(\left((8 b^2 C d^2 e^2 - 3 b^2 c C d e f - 10 b^2 B d^2 e f + 7 a b C d^2 e f - 2 b^2 c^2 C f^2 + 5 b^2 B c d f^2 - \right. \right. \\
 & \quad \left. \left. 3 a b c C d f^2 + 15 A b^2 d^2 f^2 - 10 a b B d^2 f^2 + 8 a^2 C d^2 f^2) (a+bx)^{3/2} \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \right. \right. \\
 & \quad \left. \left. \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \right) / \left(d f \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \right) + \right. \\
 & \quad \frac{1}{d f \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}}} (-bc+ad)(a+bx) \\
 & \quad \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \\
 & \quad \left(\left(8 i b^3 C d^2 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \quad \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \\
 & \quad \left(3 i b^3 c C d e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(10 i b^3 B d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(i a b^2 C d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 i b^3 c^2 C e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\left(5 i b^3 B c d e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(15 i A b^3 d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(i a^2 b C d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(2 i a b^2 c^2 C f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(5 i a b^2 B c d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(3 i a^2 b c C d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(15 \, i \, a \, A \, b^2 \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(10 \, i \, a^2 \, b \, B \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 \, i \, a^3 \, C \, d^2 \, f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(4 i b^2 C d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i b^2 c C d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5 i b^2 B d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i a b C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(\begin{aligned} & \left(i a b c c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\ & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\ & \left(15 i A b^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\ & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\ & \left(10 i a b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\ & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\ & \left(8 i a^2 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\ & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right) \end{aligned}$$

Problem 70: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} (A+Bx+Cx^2)}{(a+bx)^{3/2} \sqrt{e+fx}} dx$$

Optimal (type 4, 540 leaves, 8 steps):

$$\begin{aligned} & \left(2 (4a^2 C d f + b^2 (c C e + 3 A d f) - a b (C d e + c C f + 3 B d f)) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \right) / \\ & \left(3 b^2 (bc-ad) f (be-af) \right) - \frac{2 (A b^2 - a (b B - a C)) (c+dx)^{3/2} \sqrt{e+fx}}{b (bc-ad) (be-af) \sqrt{a+bx}} + \\ & \left(2 \sqrt{-bc+ad} (8 a^2 C d f^2 - a b f (3 C d e + c C f + 6 B d f) + b^2 (3 d f (B e + A f) - C e (2 d e - c f))) \right. \\ & \left. \sqrt{\frac{b (c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}} \right], \frac{(bc-ad) f}{d (be-af)} \right] \right) / \\ & \left(3 b^3 \sqrt{d} f^2 (be-af) \sqrt{c+dx} \sqrt{\frac{b (e+fx)}{be-af}} \right) + \\ & \left(2 \sqrt{-bc+ad} (de-cf) (2 b C e - 3 b B f + 4 a C f) \sqrt{\frac{b (c+dx)}{bc-ad}} \sqrt{\frac{b (e+fx)}{be-af}} \right. \\ & \left. \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}} \right], \frac{(bc-ad) f}{d (be-af)} \right] \right) / \left(3 b^3 \sqrt{d} f^2 \sqrt{c+dx} \sqrt{e+fx} \right) \end{aligned}$$

Result (type 4, 5168 leaves):

$$\begin{aligned} & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \left(\frac{2 C}{3 b^2 f} - \frac{2 (A b^2 - a b B + a^2 C)}{b^2 (be-af) (a+bx)} \right) + \\ & \frac{1}{3 b^4 f (be-af)} 2 \left(\left((-2 b^2 C d e^2 + b^2 c C e f + 3 b^2 B d e f - 3 a b C d e f - a b c C f^2 + 3 A b^2 d f^2 - \right. \right. \\ & \left. \left. 6 a b B d f^2 + 8 a^2 C d f^2) (a+bx)^{3/2} \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \right) / \\ & \left(d f \sqrt{c + \frac{(a+bx) (d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx) (f - \frac{af}{a+bx})}{b}} \right) + \\ & \frac{1}{d f \sqrt{c + \frac{(a+bx) (d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx) (f - \frac{af}{a+bx})}{b}}} \end{aligned}$$

$$\begin{aligned}
 & (-be+af)(a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx}\right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx}\right)} \\
 & \left(- \left(\left(2i b^3 c C d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(2i a b^2 C d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(i b^3 c^2 C e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(3i b^3 B c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(4i a b^2 c C \right. \\
 & \left. d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(3i a b^2 B d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(3 \sqrt[3]{ia^2 b c d^2 e f^2} \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(i a b^2 c^2 C f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(3 \sqrt[3]{i A b^3 c d f^3} \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(6 i a b^2 B c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(9 i a^2 b c C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i a A b^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a^2 b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i a^3 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i b^2 c C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a b C d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right], \right)$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3i b^2 B c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5i a b c C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3i A b^2 d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6i a b B d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8i a^2 C d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 71: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} (A+Bx+Cx^2)}{(a+bx)^{5/2} \sqrt{e+fx}} dx$$

Optimal (type 4, 597 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{2 (4 a^2 C f + b^2 (3 B e - 2 A f) - a b (6 C e + B f)) \sqrt{c+d x} \sqrt{e+f x}}{3 b^2 (b e - a f)^2 \sqrt{a+b x}} - \\
 & \frac{2 (A b^2 - a (b B - a C)) (c+d x)^{3/2} \sqrt{e+f x}}{3 b (b c - a d) (b e - a f) (a+b x)^{3/2}} + \left(2 \sqrt{d} (8 a^3 C d f^2 - a^2 b f (13 C d e + 7 c C f + 2 B d f) + \right. \\
 & \quad \left. a b^2 (3 C e (d e + 4 c f) + f (4 B d e + B c f - A d f)) - b^3 (A d e f + c (3 C e^2 + 3 B e f - 2 A f^2))) \right) \\
 & \sqrt{\frac{b (c+d x)}{b c - a d}} \sqrt{e+f x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+b x}}{\sqrt{-b c+a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right] \Bigg/ \\
 & \left(3 b^3 \sqrt{-b c+a d} f (b e - a f)^2 \sqrt{c+d x} \sqrt{\frac{b (e+f x)}{b e - a f}} \right) + \\
 & \left(2 (d e - c f) (4 a^2 C d f + b^2 (3 c C e + A d f) - a b (B d f + 3 C (d e + c f))) \right) \\
 & \sqrt{\frac{b (c+d x)}{b c - a d}} \sqrt{\frac{b (e+f x)}{b e - a f}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+b x}}{\sqrt{-b c+a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right] \Bigg/ \\
 & (3 b^3 \sqrt{d} \sqrt{-b c+a d} f (b e - a f) \sqrt{c+d x} \sqrt{e+f x})
 \end{aligned}$$

Result (type 4, 5074 leaves):

$$\begin{aligned}
 & \sqrt{a+b x} \sqrt{c+d x} \sqrt{e+f x} \\
 & \left(- \frac{2 (A b^2 - a b B + a^2 C)}{3 b^2 (b e - a f) (a+b x)^2} - (2 (3 b^3 B c e - 6 a b^2 c C e + A b^3 d e - 4 a b^2 B d e + 7 a^2 b C d e - \right. \\
 & \quad \left. 2 A b^3 c f - a b^2 B c f + 4 a^2 b c C f + a A b^2 d f + 2 a^2 b B d f - 5 a^3 C d f)) \Bigg/ \\
 & \left. (3 b^2 (b c - a d) (b e - a f)^2 (a+b x)) \right) - \frac{1}{3 b^4 (b c - a d) (b e - a f)^2} \\
 & 2 \left(\left((-3 b^3 c C e^2 + 3 a b^2 C d e^2 - 3 b^3 B c e f + 12 a b^2 c C e f - A b^3 d e f + 4 a b^2 B d e f - \right. \right. \\
 & \quad \left. \left. 13 a^2 b C d e f + 2 A b^3 c f^2 + a b^2 B c f^2 - 7 a^2 b c C f^2 - a A b^2 d f^2 - 2 a^2 b B d f^2 + 8 a^3 C d f^2) \right. \right. \\
 & \quad \left. (a+b x)^{3/2} \left(d + \frac{b c}{a+b x} - \frac{a d}{a+b x} \right) \left(f + \frac{b e}{a+b x} - \frac{a f}{a+b x} \right) \right) \Bigg/ \\
 & \left(f \sqrt{c + \frac{(a+b x) \left(d - \frac{a d}{a+b x} \right)}{b}} \sqrt{e + \frac{(a+b x) \left(f - \frac{a f}{a+b x} \right)}{b}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{f \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \\
 & (bc-ad)(-be+af)(a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx}\right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx}\right)} \\
 & \left(\left(3 i b^3 c C e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/ \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(3 i a b^2 C d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/ \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(3 i b^3 B c e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg/ \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(12 i a b^2 c C e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(i A b^3 d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(4 i a b^2 B d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(13 i a^2 b c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 i A b^3 c f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(i a b^2 B c f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(7 i a^2 b c c f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(i a A b^2 d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(2 i a^2 b B d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(8 i a^3 C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i b^2 c C e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i b^2 B d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(9 i a b C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(3 i a b c C f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i A b^2 d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(2 i a b B d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i a^2 C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right)$$

Problem 72: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{c+dx} (A+Bx+Cx^2)}{(a+bx)^{7/2} \sqrt{e+fx}} dx$$

Optimal (type 4, 1034 leaves, 9 steps):

$$\begin{aligned} & \left(2 (4a^3 C d f - b^3 (5B c e - 2A d e - 4A c f) + \right. \\ & \quad \left. a b^2 (10 c C e + 3 B d e + B c f - 6 A d f) - a^2 b (8 C d e + 6 c C f - B d f) \right) \sqrt{c+dx} \sqrt{e+fx} \Big/ \\ & \left(15 b^2 (b c - a d) (b e - a f)^2 (a+bx)^{3/2} - \left(2 (8 a^4 C d^2 f^2 - a^3 b d f (23 C d e + 13 c C f - 2 B d f) - \right. \right. \\ & \quad \left. \left. b^4 (2 A d^2 e^2 - c d e (5 B e - 3 A f) - c^2 (15 C e^2 - 10 B e f + 8 A f^2)) - \right. \right. \\ & \quad \left. \left. a^2 b^2 (d f (7 B d e + 2 B c f - 3 A d f) - C (23 d^2 e^2 + 37 c d e f + 3 c^2 f^2)) - \right. \right. \\ & \quad \left. \left. a b^3 (d^2 e (3 B e - 7 A f) + 2 c^2 f (5 C e - B f) + c d (40 C e^2 - 13 f (B e - A f))) \right) \right) \\ & \quad \left. \sqrt{c+dx} \sqrt{e+fx} \right) \Big/ \left(15 b^2 (b c - a d)^2 (b e - a f)^3 \sqrt{a+bx} \right) - \\ & \frac{2 (A b^2 - a (b B - a C)) (c+dx)^{3/2} \sqrt{e+fx}}{5 b (b c - a d) (b e - a f) (a+bx)^{5/2}} + \\ & \frac{1}{15 b^3 (-b c + a d)^{3/2} (b e - a f)^3 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{b e - a f}}} \\ & \frac{2 \sqrt{d} (8 a^4 C d^2 f^2 - a^3 b d f (23 C d e + 13 c C f - 2 B d f) - b^4 (2 A d^2 e^2 - c d e (5 B e - 3 A f) - c^2 (15 C e^2 - 10 B e f + 8 A f^2)) - a^2 b^2 (d f (7 B d e + 2 B c f - 3 A d f) - C (23 d^2 e^2 + 37 c d e f + 3 c^2 f^2)) - a b^3 (d^2 e (3 B e - 7 A f) + 2 c^2 f (5 C e - B f) + c d (40 C e^2 - 13 f (B e - A f)))}{\sqrt{\frac{b(c+dx)}{b c - a d}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-b c + a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right]} + \\ & \left(2 \sqrt{d} (d e - c f) (4 a^3 C d f - b^3 (5 B c e - 2 A d e - 4 A c f) + \right. \\ & \quad \left. a b^2 (10 c C e + 3 B d e + B c f - 6 A d f) - a^2 b (8 C d e + 6 c C f - B d f) \right) \\ & \quad \left. \sqrt{\frac{b(c+dx)}{b c - a d}} \sqrt{\frac{b(e+fx)}{b e - a f}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-b c + a d}}\right], \frac{(b c - a d) f}{d (b e - a f)}\right] \right) \Big/ \\ & \left(15 b^3 (-b c + a d)^{3/2} (b e - a f)^2 \sqrt{c+dx} \sqrt{e+fx} \right) \end{aligned}$$

Result (type 4, 9186 leaves):

$$\begin{aligned} & \frac{\sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx}}{\left(-\frac{2 (A b^2 - a b B + a^2 C)}{5 b^2 (b e - a f) (a+bx)^3} - \left(2 (5 b^3 B c e - 10 a b^2 c C e + A b^3 d e - 6 a b^2 B d e + 11 a^2 b C d e - \right. \right. \\ & \quad \left. \left. 4 A b^3 c f - a b^2 B c f + 6 a^2 b c C f + 3 a A b^2 d f + 2 a^2 b B d f - 7 a^3 C d f) \right) \right) \Big/ \\ & \left(15 b^2 (b c - a d) (b e - a f)^2 (a+bx)^2 \right) - \frac{1}{15 b^2 (b c - a d)^2 (b e - a f)^3 (a+bx)} \end{aligned}$$

$$\begin{aligned}
 & 2 \left(15 b^4 c^2 C e^2 + 5 b^4 B c d e^2 - 40 a b^3 c C d e^2 - 2 A b^4 d^2 e^2 - 3 a b^3 B d^2 e^2 + 23 a^2 b^2 C d^2 e^2 - \right. \\
 & \quad 10 b^4 B c^2 e f - 10 a b^3 c^2 C e f - 3 A b^4 c d e f + 13 a b^3 B c d e f + 37 a^2 b^2 c C d e f + \\
 & \quad 7 a A b^3 d^2 e f - 7 a^2 b^2 B d^2 e f - 23 a^3 b c d^2 e f + 8 A b^4 c^2 f^2 + 2 a b^3 B c^2 f^2 + 3 a^2 b^2 c^2 C f^2 - \\
 & \quad \left. 13 a A b^3 c d f^2 - 2 a^2 b^2 B c d f^2 - 13 a^3 b c C d f^2 + 3 a^2 A b^2 d^2 f^2 + 2 a^3 b B d^2 f^2 + 8 a^4 C d^2 f^2 \right) + \\
 & \frac{1}{15 b^4 (b c - a d)^2 (b e - a f)^3} 2 d \left(\frac{1}{d \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} \right. \\
 & \quad \left(15 b^4 c^2 C e^2 + 5 b^4 B c d e^2 - 40 a b^3 c C d e^2 - 2 A b^4 d^2 e^2 - 3 a b^3 B d^2 e^2 + 23 a^2 b^2 C d^2 e^2 - \right. \\
 & \quad 10 b^4 B c^2 e f - 10 a b^3 c^2 C e f - 3 A b^4 c d e f + 13 a b^3 B c d e f + 37 a^2 b^2 c C d e f + \\
 & \quad 7 a A b^3 d^2 e f - 7 a^2 b^2 B d^2 e f - 23 a^3 b c d^2 e f + 8 A b^4 c^2 f^2 + 2 a b^3 B c^2 f^2 + 3 a^2 b^2 c^2 C f^2 - \\
 & \quad \left. 13 a A b^3 c d f^2 - 2 a^2 b^2 B c d f^2 - 13 a^3 b c C d f^2 + 3 a^2 A b^2 d^2 f^2 + 2 a^3 b B d^2 f^2 + 8 a^4 C d^2 f^2 \right) \\
 & \quad \left. (a+bx)^{3/2} \left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) + \right. \\
 & \quad \left. \frac{1}{d \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}} (-bc+ad)(be-af)(a+bx) \right. \\
 & \quad \left. \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)} \right) \\
 & \left(\left(15 i b^4 c^2 C e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\
 & \quad \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \Bigg) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} + \right. \\
 & \quad \left. \left(5 i b^4 B c d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc+ad}}{\sqrt{a+bx}} \right] \right], \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - 40 \text{i} a b^3 c \right.$$

$$\left. c d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(2 \text{i} A b^4 d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(3 \text{i} a b^3 B d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(23 \text{i} a^2 b^2 c \right.$$

$$d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(10 \text{i} b^4 B c^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(10 \text{i} a b^3 c^2 \right.$$

$$c e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(3 \text{i} A b^4 c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(13 \text{i} a b^3 B \right. \right.$$

$$\left. \left. c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(37 \text{i} a^2 b^2 c \right. \right.$$

$$\left. \left. c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(7 \text{i} a A b^3 d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(7 \text{i} a^2 b^2 B \right.$$

$$\left. d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(23 \text{i} a^3 b C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} + \right.$$

$$\left. 8 i A b^4 c^2 f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} + \right.$$

$$\left. 2 i a b^3 B c^2 f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} + \right.$$

$$\left(3 \, i \, a^2 \, b^2 \, c^2 \, C \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(13 \, i \, a \, A \, b^3 \, c \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 \, i \, a^2 \, b^2 \, B \, c \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(13 i a^3 b c C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(3 i a^2 A b^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(2 i a^3 b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) +$$

$$\left(8 i a^4 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(15 i b^3 c C d e^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i a b^2 C d^2 e^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(5 i b^3 B c d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(20 i a b^2 c C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(i A b^3 d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(6 i a b^2 B d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(19 i a^2 b C d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(4 \, i \, A b^3 c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(i \, a b^2 B c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \left(9 \, i \, a^2 b c C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \left(3 \, i \, a A b^2 d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + \right.$$

$$\left(2 i a^2 b B d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 i a^3 C d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \Bigg)$$

Problem 73: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a+bx)^{3/2} (A+Bx+Cx^2)}{\sqrt{c+dx} \sqrt{e+fx}} dx$$

Optimal (type 4, 838 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{105 b d^3 f^3} 2 (5 b d f (5 b c C e + a C d e + a c C f - 7 A b d f) + \\
 & \quad (3 a d f - 4 b (d e + c f)) (2 a C d f - b (7 B d f - 6 C (d e + c f)))) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} - \\
 & \quad \frac{2 (2 a C d f - b (7 B d f - 6 C (d e + c f))) (a+bx)^{3/2} \sqrt{c+dx} \sqrt{e+fx}}{35 b d^2 f^2} + \\
 & \quad \frac{2 C (a+bx)^{5/2} \sqrt{c+dx} \sqrt{e+fx}}{7 b d f} - \frac{1}{105 b^2 d^{7/2} f^4 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}} \\
 & \quad 2 \sqrt{-bc+ad} \left(3 b d f (5 a d f (5 b c C e + a C d e + a c C f - 7 A b d f) - \right. \\
 & \quad \quad (3 b c e + a d e + a c f) (2 a C d f - b (7 B d f - 6 C (d e + c f)))) + \\
 & \quad \quad \left. 2 \left(\frac{a d f}{2} - b (d e + c f) \right) (5 b d f (5 b c C e + a C d e + a c C f - 7 A b d f) + \right. \\
 & \quad \quad \left. (3 a d f - 4 b (d e + c f)) (2 a C d f - b (7 B d f - 6 C (d e + c f)))) \right) \\
 & \quad \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] - \\
 & \quad \frac{1}{105 b^2 d^{7/2} f^4 \sqrt{c+dx} \sqrt{e+fx}} 2 \sqrt{-bc+ad} (be-af) (3 a^2 C d^2 f^2 (de-cf) - \\
 & \quad \quad 3 a b d f (7 d f (3 B d e + 2 B c f - 5 A d f) - C (16 d^2 e^2 + 8 c d e f + 11 c^2 f^2)) - \\
 & \quad \quad b^2 (C (48 d^3 e^3 + 16 c d^2 e^2 f + 17 c^2 d e f^2 + 24 c^3 f^3) + \\
 & \quad \quad 7 d f (5 A d f (2 d e + c f) - B (8 d^2 e^2 + 3 c d e f + 4 c^2 f^2)))) \\
 & \quad \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right]
 \end{aligned}$$

Result (type 4, 7300 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\
 & \left(\frac{1}{105 b d^3 f^3} 2 (24 b^2 C d^2 e^2 + 23 b^2 c C d e f - 28 b^2 B d^2 e f - 33 a b C d^2 e f + 24 b^2 c^2 C f^2 - \right. \\
 & \quad 28 b^2 B c d f^2 - 33 a b c C d f^2 + 35 A b^2 d^2 f^2 + 42 a b B d^2 f^2 + 3 a^2 C d^2 f^2) + \\
 & \quad \left. \frac{2 (-6 b C d e - 6 b c C f + 7 b B d f + 8 a C d f) x}{35 d^2 f^2} + \frac{2 b C x^2}{7 d f} \right) + \\
 & \frac{1}{105 b^3 d^3 f^3} 2 \left(\frac{1}{d f \sqrt{c + \frac{(a+bx)(d-ad)}{b}} \sqrt{e + \frac{(a+bx)(f-af)}{b}}} \right. \\
 & \quad (-48 b^3 C d^3 e^3 - 40 b^3 c C d^2 e^2 f + 56 b^3 B d^3 e^2 f + 72 a b^2 C d^3 e^2 f - 40 b^3 c^2 C d e f^2 + \\
 & \quad 49 b^3 B c d^2 e f^2 + 62 a b^2 c C d^2 e f^2 - 70 A b^3 d^3 e f^2 - 91 a b^2 B d^3 e f^2 - 12 a^2 b C d^3 e f^2 - \\
 & \quad 48 b^3 c^3 C f^3 + 56 b^3 B c^2 d f^3 + 72 a b^2 c^2 C d f^3 - 70 A b^3 c d^2 f^3 - 91 a b^2 B c d^2 f^3 - \\
 & \quad \left. 12 a^2 b c C d^2 f^3 + 140 a A b^2 d^3 f^3 + 21 a^2 b B d^3 f^3 - 6 a^3 C d^3 f^3) (a+bx)^{3/2} \right)
 \end{aligned}$$

$$\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) + \frac{1}{df \sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}}}$$

$$(-bc+ad)(-be+af)(a+bx) \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx} \right)}$$

$$\left(\left(48 i b^3 C d^3 e^3 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(40 i b^3 c c \right.$$

$$d^2 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(56 i b^3 B d^3 e^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(72 i a b^2 C \right.$$

$$d^3 e^2 f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(40 i b^3 c^2 C \right.$$

$$d e f^3 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(49 i b^3 B c \right.$$

$$\begin{aligned}
 & d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(62 i a b^2 c C \right. \\
 & d^2 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(70 i A b^3 d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(91 i a b^2 B \right.
 \end{aligned}$$

$$\begin{aligned}
 & d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(12 i a^2 b c d^3 e f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(48 i b^3 c^3 C f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(56 i b^3 B c^2 d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(72 i a b^2 c^2 C d f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left. \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(70 i A b^3 c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(91 i a b^2 B c d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(12 i a^2 b c C d^2 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(140 i a A b^2 d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right. \\
 & \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(21 i a^2 b B d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(6 i a^3 C d^3 f^4 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(24 i b^2 C d^3 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right.$$

$$\left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(23 i b^2 c C d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(28 i b^2 B d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left. \left. \left. \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(15 i a b C d^3 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right.$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \left(24 i b^2 c^2 C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(28 i b^2 B c d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \left(15 i a b c C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \right)$$

$$\left(\sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(35 i A b^2 d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(21 i a b B d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(6 i a^2 C d^3 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) \right) \right)$$

Problem 74: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+bx} (A+Bx+Cx^2)}{\sqrt{c+dx} \sqrt{e+fx}} dx$$

Optimal (type 4, 528 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{2 (2 a C d f - b (5 B d f - 4 C (d e + c f))) \sqrt{a+b x} \sqrt{c+d x} \sqrt{e+f x}}{15 b d^2 f^2} + \\
 & \frac{2 C (a+b x)^{3/2} \sqrt{c+d x} \sqrt{e+f x}}{5 b d f} - \left(2 \sqrt{-b c+a d} (3 b d f (3 b c C e+a C d e+a c C f-5 A b d f) + \right. \\
 & \quad \left. (a d f-2 b (d e+c f)) (2 a C d f-b (5 B d f-4 C (d e+c f)))) \right) \\
 & \sqrt{\frac{b(c+d x)}{b c-a d}} \sqrt{e+f x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+b x}}{\sqrt{-b c+a d}}\right], \frac{(b c-a d) f}{d(b e-a f)}\right] / \\
 & \left(15 b^2 d^{5/2} f^3 \sqrt{c+d x} \sqrt{\frac{b(e+f x)}{b e-a f}} - \left(2 \sqrt{-b c+a d} (b e-a f) \right. \right. \\
 & \quad \left. \left. (a C d f (d e-c f)-b (5 d f (2 B d e+B c f-3 A d f)-C (8 d^2 e^2+3 c d e f+4 c^2 f^2))) \right) \right) \\
 & \sqrt{\frac{b(c+d x)}{b c-a d}} \sqrt{\frac{b(e+f x)}{b e-a f}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+b x}}{\sqrt{-b c+a d}}\right], \frac{(b c-a d) f}{d(b e-a f)}\right] / \\
 & (15 b^2 d^{5/2} f^3 \sqrt{c+d x} \sqrt{e+f x})
 \end{aligned}$$

Result (type 4, 3657 leaves):

$$\begin{aligned}
 & \sqrt{a+b x} \sqrt{c+d x} \left(\frac{2 (-4 b C d e-4 b c C f+5 b B d f+a C d f)}{15 b d^2 f^2} + \frac{2 C x}{5 d f} \right) \sqrt{e+f x} - \\
 & \frac{1}{15 b^3 d^2 f^2} 2 \left(\left((-8 b^2 C d^2 e^2-7 b^2 c C d e f+10 b^2 B d^2 e f+3 a b C d^2 e f-8 b^2 c^2 C f^2+10 b^2 B c d f^2+ \right. \right. \\
 & \quad \left. \left. 3 a b c C d f^2-15 A b^2 d^2 f^2-5 a b B d^2 f^2+2 a^2 C d^2 f^2) (a+b x)^{3/2} \left(d+\frac{b c}{a+b x}-\frac{a d}{a+b x} \right) \right. \right. \\
 & \quad \left. \left. \left(f+\frac{b e}{a+b x}-\frac{a f}{a+b x} \right) \right) \right) / \left(d f \sqrt{c+\frac{(a+b x)\left(d-\frac{a d}{a+b x}\right)}{b}} \sqrt{e+\frac{(a+b x)\left(f-\frac{a f}{a+b x}\right)}{b}} \right) + \\
 & \frac{1}{d f \sqrt{c+\frac{(a+b x)\left(d-\frac{a d}{a+b x}\right)}{b}} \sqrt{e+\frac{(a+b x)\left(f-\frac{a f}{a+b x}\right)}{b}}} (-b c+a d) (-b e+a f) \\
 & (a+b x) \sqrt{\left(d+\frac{b c}{a+b x}-\frac{a d}{a+b x} \right) \left(f+\frac{b e}{a+b x}-\frac{a f}{a+b x} \right)}
 \end{aligned}$$

$$\left(\left(8 i b^2 c d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \right. \\ \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\ \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) + \\ \left(7 i b^2 c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \\ \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\ \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) - \\ \left(10 i b^2 B d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right), \right. \right. \\ \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right] \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \\ \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(3 \, i \, a \, b \, C \, d^2 \, e \, f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(8 \, i \, b^2 \, c^2 \, C \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(10 \, i \, b^2 \, B \, c \, d \, f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \, \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\begin{aligned}
 & \left(3 \sqrt[3]{i a b c C d f^3} \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(15 \sqrt[3]{i A b^2 d^2 f^3} \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \\
 & \left(5 \sqrt[3]{i a b B d^2 f^3} \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left(2 i a^2 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(4 i b C d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(4 i b C C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(5 i b B d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i a C d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right)$$

Problem 75: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{A + Bx + Cx^2}{\sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx}} dx$$

Optimal (type 4, 387 leaves, 7 steps):

$$\frac{2C\sqrt{a+bx}\sqrt{c+dx}\sqrt{e+fx}}{3bdf}$$

$$\left(2\sqrt{-bc+ad} (2aCdf - b(3Bdf - 2C(de+cf))) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \right.$$

$$\left. \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \right) / \left(3b^2 d^{3/2} f^2 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}} \right) +$$

$$\left(2\sqrt{-bc+ad} (aCf(de-cf) - b(3df(Be-Af) - Ce(2de+cf))) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \right) / (3b^2 d^{3/2} f^2 \sqrt{c+dx} \sqrt{e+fx})$$

Result (type 4, 418 leaves):

$$\frac{1}{3 b^3 d^2 f^2 \sqrt{c+dx} \sqrt{e+fx}} \sqrt{a+bx} \left(2 b^2 C d f (c+dx) (e+fx) - \frac{2 b^2 (-3 b B d f + 2 a C d f + 2 b C (d e + c f)) (c+dx) (e+fx)}{a+bx} + 2 i \sqrt{-a + \frac{bc}{d}} d f (3 b B d f - 2 a C d f - 2 b C (d e + c f)) \sqrt{a+bx} \sqrt{\frac{b(c+dx)}{d(a+bx)}} \sqrt{\frac{b(e+fx)}{f(a+bx)}} \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-a + \frac{bc}{d}}}{\sqrt{a+bx}}\right], \frac{b d e - a d f}{b c f - a d f}\right] + \frac{1}{\sqrt{-a + \frac{bc}{d}}} 2 i b f (a C d (-d e + c f) + b (2 c^2 C f + 3 A d^2 f + c d (C e - 3 B f))) \sqrt{a+bx} \sqrt{\frac{b(c+dx)}{d(a+bx)}} \sqrt{\frac{b(e+fx)}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-a + \frac{bc}{d}}}{\sqrt{a+bx}}\right], \frac{b d e - a d f}{b c f - a d f}\right] \right)$$

Problem 76: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{A + Bx + Cx^2}{(a+bx)^{3/2} \sqrt{c+dx} \sqrt{e+fx}} dx$$

Optimal (type 4, 422 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2 (Ab^2 - a (bB - aC)) \sqrt{c+dx} \sqrt{e+fx}}{b (bc - ad) (be - af) \sqrt{a+bx}} - \\
 & \left(2 (2a^2 Cdf + b^2 (cCe + Adf) - ab (Cde + cCf + Bdf)) \right. \\
 & \left. \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \right) / \\
 & \left(b^2 \sqrt{d} \sqrt{-bc+ad} f (be-af) \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}} \right) - \\
 & \left(2 (aC (de - cf) - b (cCe - Bcf + Adf)) \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right] \right) / (b^2 \sqrt{d} \sqrt{-bc+ad} f \sqrt{c+dx} \sqrt{e+fx})
 \end{aligned}$$

Result (type 4, 477 leaves):

$$\frac{1}{b^3 (bc - ad) (be - af) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx}}$$

$$2 \left(-b^2 (Ab^2 + a(-bB + aC)) (c+dx) (e+fx) + \frac{1}{df} \right.$$

$$b^2 (2a^2 Cdf + b^2 (cCe + Adf) - ab (Cde + cCf + Bdf)) (c+dx) (e+fx) + \frac{1}{\sqrt{-a + \frac{bc}{d} d}}$$

$$\left. i (bc - ad) (2a^2 Cdf + b^2 (cCe + Adf) - ab (Cde + cCf + Bdf)) (a+bx)^{3/2} \right.$$

$$\left. \sqrt{\frac{b(c+dx)}{d(a+bx)}} \sqrt{\frac{b(e+fx)}{f(a+bx)}} \operatorname{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-a + \frac{bc}{d}}}{\sqrt{a+bx}} \right], \frac{bde - adf}{bcf - adf} \right] + \right.$$

$$\left. \frac{1}{\sqrt{-a + \frac{bc}{d} d}} i b (-bc + ad) (aC (de - cf) + b (cCe - Bde + Adf)) (a+bx)^{3/2} \right.$$

$$\left. \sqrt{\frac{b(c+dx)}{d(a+bx)}} \sqrt{\frac{b(e+fx)}{f(a+bx)}} \operatorname{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-a + \frac{bc}{d}}}{\sqrt{a+bx}} \right], \frac{bde - adf}{bcf - adf} \right] \right)$$

Problem 77: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + Bx + Cx^2}{(a+bx)^{5/2} \sqrt{c+dx} \sqrt{e+fx}} dx$$

Optimal (type 4, 642 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{2 (Ab^2 - a (bB - aC)) \sqrt{c+dx} \sqrt{e+fx}}{3b (bc - ad) (be - af) (a+bx)^{3/2}} + \\
 & \left(\frac{2 (2a^3 Cdf + ab^2 (6cCe + Bde + Bcf - 4Adf) - b^3 (3Bce - 2A(de + cf)) + a^2 b (Bdf - 4C(de + cf))) \sqrt{c+dx} \sqrt{e+fx}}{(3b (bc - ad))^2 (be - af)^2 \sqrt{a+bx}} \right) - \\
 & \left(\frac{2\sqrt{d} (2a^3 Cdf + ab^2 (6cCe + Bde + Bcf - 4Adf) - b^3 (3Bce - 2A(de + cf)) + a^2 b (Bdf - 4C(de + cf))) \sqrt{\frac{b(c+dx)}{bc-ad}}}{\sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right]} \right) / \\
 & \left(\frac{3b^2 (-bc+ad)^{3/2} (be-af)^2 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}}{2 (a^2 Cd (de - cf) - b^2 (3c^2 Ce - 3Bcde + 2Ad^2 e + Acdf) + ab (3 (c^2 C + Ad^2) f - Bd (de + 2cf))) \sqrt{\frac{b(c+dx)}{bc-ad}}} \right) - \\
 & \left(\frac{\sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d}\sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad)f}{d(be-af)}\right]}{(3b^2 \sqrt{d} (-bc+ad)^{3/2} (be-af) \sqrt{c+dx} \sqrt{e+fx})} \right) /
 \end{aligned}$$

Result (type 4, 4349 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\
 & \left(- \frac{2 (Ab^2 - abB + a^2 C)}{3b (bc - ad) (be - af) (a+bx)^2} - (2 (3b^3 Bce - 6ab^2 cCe - 2Ab^3 de - ab^2 Bde + 4a^2 bCde - 2Ab^3 cf - ab^2 Bcf + 4a^2 bcCf + 4aAb^2 df - a^2 bBdf - 2a^3 Cdf)) / \right. \\
 & \left. (3b (bc - ad))^2 (be - af)^2 (a+bx) \right) + \frac{1}{3b^3 (bc - ad)^2 (be - af)^2} \\
 & 2 \left((3b^3 Bce - 6ab^2 cCe - 2Ab^3 de - ab^2 Bde + 4a^2 bCde - 2Ab^3 cf - ab^2 Bcf +
 \end{aligned}$$

$$\begin{aligned}
 & 4 a^2 b c C f + 4 a A b^2 d f - a^2 b B d f - 2 a^3 C d f) (a + b x)^{3/2} \left(d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \\
 & \left(f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right) \Bigg/ \left(\sqrt{c + \frac{(a + b x) \left(d - \frac{a d}{a + b x} \right)}{b}} \sqrt{e + \frac{(a + b x) \left(f - \frac{a f}{a + b x} \right)}{b}} \right) - \\
 & \frac{1}{\sqrt{c + \frac{(a + b x) \left(d - \frac{a d}{a + b x} \right)}{b}} \sqrt{e + \frac{(a + b x) \left(f - \frac{a f}{a + b x} \right)}{b}}} (b c - a d) (b e - a f) (a + b x) \\
 & \sqrt{\left(d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \left(f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right)} \\
 & \left(\left(3 i b^3 B c e f \sqrt{1 - \frac{-b c + a d}{d (a + b x)}} \sqrt{1 - \frac{-b e + a f}{f (a + b x)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-b c + a d}}{\sqrt{a + b x}} \right], \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{d (-b e + a f)}{(-b c + a d) f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-b c + a d}}{\sqrt{a + b x}} \right], \frac{d (-b e + a f)}{(-b c + a d) f} \right] \right) \right) \Bigg/ \\
 & \left(\sqrt{-\frac{-b c + a d}{d}} (-b e + a f) \sqrt{\left(d + \frac{b c - a d}{a + b x} \right) \left(f + \frac{b e - a f}{a + b x} \right)} \right) - \\
 & \left(6 i a b^2 c C e f \sqrt{1 - \frac{-b c + a d}{d (a + b x)}} \sqrt{1 - \frac{-b e + a f}{f (a + b x)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-b c + a d}}{\sqrt{a + b x}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{d (-b e + a f)}{(-b c + a d) f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-b c + a d}}{\sqrt{a + b x}} \right], \frac{d (-b e + a f)}{(-b c + a d) f} \right] \right) \right) \Bigg/ \\
 & \left(\sqrt{-\frac{-b c + a d}{d}} (-b e + a f) \sqrt{\left(d + \frac{b c - a d}{a + b x} \right) \left(f + \frac{b e - a f}{a + b x} \right)} \right) -
 \end{aligned}$$

$$\left(2 i A b^3 d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a b^2 B d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(4 i a^2 b C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i A b^3 c f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a b^2 B c f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(4 i a^2 b c C f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(4 i a A b^2 d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a^2 b B d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(2 i a^3 C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 i b^2 c C e \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(3 i a b C d e \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(3 i a b c C f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i A b^2 d f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(i a b B d f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) -$$

$$\left(2 i a^2 C d f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx} \right) \left(f + \frac{be-af}{a+bx} \right)} \right) \right)$$

Problem 78: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + Bx + Cx^2}{(a + bx)^{7/2} \sqrt{c + dx} \sqrt{e + fx}} dx$$

Optimal (type 4, 1116 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 (A b^2 - a (b B - a C)) \sqrt{c+dx} \sqrt{e+fx}}{5 b (b c - a d) (b e - a f) (a + b x)^{5/2}} + \\
 & \left(2 (2 a^3 C d f + a b^2 (10 c C e + B d e + B c f - 8 A d f)) - b^3 (5 B c e - 4 A (d e + c f)) + \right. \\
 & \quad \left. 3 a^2 b (B d f - 2 C (d e + c f)) \right) \sqrt{c+dx} \sqrt{e+fx} / \\
 & \left(15 b (b c - a d)^2 (b e - a f)^2 (a + b x)^{3/2} + (2 (2 a^4 C d^2 f^2 + a^3 b d f (3 B d f - 7 C (d e + c f)) - \right. \\
 & \quad b^4 (8 A d^2 e^2 - c d e (10 B e - 7 A f) + c^2 (15 C e^2 - 10 B e f + 8 A f^2)) - \\
 & \quad a b^3 (d^2 e (2 B e - 23 A f) - 2 c^2 f (5 C e - B f) - c d (10 C e^2 - 33 B e f + 23 A f^2)) - \\
 & \quad \left. a^2 b^2 (C (3 d^2 e^2 - 13 c d e f + 3 c^2 f^2) + d f (23 A d f - 7 B (d e + c f))) \right) \sqrt{c+dx} \sqrt{e+fx} / \\
 & \left(15 b (b c - a d)^3 (b e - a f)^3 \sqrt{a+bx} \right) + \frac{1}{15 b^2 (-bc+ad)^{5/2} (be-af)^3 \sqrt{c+dx} \sqrt{\frac{b(e+fx)}{be-af}}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{d} (2 a^4 C d^2 f^2 + a^3 b d f (3 B d f - 7 C (d e + c f)) - \\
 & \quad b^4 (8 A d^2 e^2 - c d e (10 B e - 7 A f) + c^2 (15 C e^2 - 10 B e f + 8 A f^2)) - \\
 & \quad a b^3 (d^2 e (2 B e - 23 A f) - 2 c^2 f (5 C e - B f) - c d (10 C e^2 - 33 B e f + 23 A f^2)) - \\
 & \quad a^2 b^2 (C (3 d^2 e^2 - 13 c d e f + 3 c^2 f^2) + d f (23 A d f - 7 B (d e + c f)))
 \end{aligned}$$

$$\sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{e+fx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right] +$$

$$\begin{aligned}
 & \frac{1}{15 b^2 (-bc+ad)^{5/2} (be-af)^2 \sqrt{c+dx} \sqrt{e+fx}} \\
 & 2 \sqrt{d} (a^3 C d f (d e - c f) + b^3 (8 A d^2 e^2 - c d e (10 B e - 3 A f) + c^2 (15 C e^2 - 5 B e f + 4 A f^2)) + \\
 & \quad a b^2 (d^2 e (2 B e - 19 A f) - c^2 f (20 C e - B f) - c d (10 C e^2 - 27 B e f + 11 A f^2)) - \\
 & \quad 3 a^2 b (d f (2 B d e + 3 B c f - 5 A d f) - C (d^2 e^2 + c d e f + 3 c^2 f^2))) \\
 & \sqrt{\frac{b(c+dx)}{bc-ad}} \sqrt{\frac{b(e+fx)}{be-af}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} \sqrt{a+bx}}{\sqrt{-bc+ad}}\right], \frac{(bc-ad) f}{d (be-af)}\right]
 \end{aligned}$$

Result (type 4, 8844 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \\
 & \left(- \frac{2 (A b^2 - a b B + a^2 C)}{5 b (b c - a d) (b e - a f) (a + b x)^3} - (2 (5 b^3 B c e - 10 a b^2 c C e - 4 A b^3 d e - a b^2 B d e + \right. \\
 & \quad \left. 6 a^2 b C d e - 4 A b^3 c f - a b^2 B c f + 6 a^2 b c C f + 8 a A b^2 d f - 3 a^2 b B d f - 2 a^3 C d f)) / \right. \\
 & \quad \left. (15 b (b c - a d)^2 (b e - a f)^2 (a + b x)^2) - \frac{1}{15 b (b c - a d)^3 (b e - a f)^3 (a + b x)} \right. \\
 & \quad \left. 2 (15 b^4 c^2 C e^2 - 10 b^4 B c d e^2 - 10 a b^3 c C d e^2 + 8 A b^4 d^2 e^2 + 2 a b^3 B d^2 e^2 + 3 a^2 b^2 C d^2 e^2 - \right. \\
 & \quad 10 b^4 B c^2 e f - 10 a b^3 c^2 C e f + 7 A b^4 c d e f + 33 a b^3 B c d e f - 13 a^2 b^2 c C d e f - \\
 & \quad 23 a A b^3 d^2 e f - 7 a^2 b^2 B d^2 e f + 7 a^3 b C d^2 e f + 8 A b^4 c^2 f^2 + 2 a b^3 B c^2 f^2 + 3 a^2 b^2 c^2 C f^2 - \\
 & \quad \left. 23 a A b^3 c d f^2 - 7 a^2 b^2 B c d f^2 + 7 a^3 b c C d f^2 + 23 a^2 A b^2 d^2 f^2 - 3 a^3 b B d^2 f^2 - 2 a^4 C d^2 f^2) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{15 b^3 (bc - ad)^3 (be - af)^3} 2df \left(\frac{1}{df \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}}} \right. \\
 & (15 b^4 c^2 C e^2 - 10 b^4 B c d e^2 - 10 a b^3 c C d e^2 + 8 A b^4 d^2 e^2 + 2 a b^3 B d^2 e^2 + 3 a^2 b^2 C d^2 e^2 - \\
 & 10 b^4 B c^2 e f - 10 a b^3 c^2 C e f + 7 A b^4 c d e f + 33 a b^3 B c d e f - 13 a^2 b^2 c C d e f - \\
 & 23 a A b^3 d^2 e f - 7 a^2 b^2 B d^2 e f + 7 a^3 b c d^2 e f + 8 A b^4 c^2 f^2 + 2 a b^3 B c^2 f^2 + 3 a^2 b^2 c^2 C f^2 - \\
 & 23 a A b^3 c d f^2 - 7 a^2 b^2 B c d f^2 + 7 a^3 b c c d f^2 + 23 a^2 A b^2 d^2 f^2 - 3 a^3 b B d^2 f^2 - 2 a^4 C d^2 f^2) \\
 & (a + bx)^{3/2} \left(d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left(f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) + \\
 & \frac{1}{df \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}}} (-bc + ad) (-be + af) (a + bx) \\
 & \sqrt{\left(d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left(f + \frac{be}{a + bx} - \frac{af}{a + bx} \right)} \left(- \left(\left(15 i b^4 c^2 C e^2 f \sqrt{1 - \frac{-bc + ad}{d(a + bx)}} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 - \frac{-be + af}{f(a + bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc + ad}}{\sqrt{a + bx}} \right], \frac{d(-be + af)}{(-bc + ad)f} \right] - \right. \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc + ad}}{\sqrt{a + bx}} \right], \frac{d(-be + af)}{(-bc + ad)f} \right] \right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc + ad}{d}} (-be + af) \sqrt{\left(d + \frac{bc - ad}{a + bx} \right) \left(f + \frac{be - af}{a + bx} \right)} \right) + \\
 & \left(10 i b^4 B c d e^2 f \sqrt{1 - \frac{-bc + ad}{d(a + bx)}} \sqrt{1 - \frac{-be + af}{f(a + bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-bc + ad}}{\sqrt{a + bx}} \right], \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} + 10 \text{i} a b^3 c \right.$$

$$C d e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(8 \text{i} A b^4 d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} - \right.$$

$$\left. \left(2 \text{i} a b^3 B d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(3 \text{i} a^2 b^2 c \right.$$

$$d^2 e^2 f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(10 \text{i} b^4 B c^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) + \left(10 \text{i} a b^3 c^2 \right.$$

$$c e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(7 \text{i} A b^4 c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \left(33 \text{i} a b^3 B$$

$$c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(13 \text{i} a^2 b^2 c c d e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(23 i a A b^3 d^2 e f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\left. \text{EllipticF} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) /$$

$$\left(\sqrt{-\frac{bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(7 i a^2 b^2 B d^2 e f^2 \sqrt{1 - \frac{bc+ad}{d(a+bx)}} \sqrt{1 - \frac{be+af}{f(a+bx)}} \right)$$

$$\left(\text{EllipticE} \left[i \operatorname{ArcSinh} \left[\frac{\sqrt{-\frac{bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right)\right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(7 \text{i} a^3 b c d^2 e f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(8 \text{i} A b^4 c^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f}\right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) / \\
 & \left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) - \\
 & \left(2 \text{i} a b^3 B c^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(3 \text{i} a^2 b^2 c^2 c f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(23 \text{i} a A b^3 c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \frac{d(-be+af)}{(-bc+ad)f}\right]\right) \right) \right) \right/$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(7 \text{i} a^2 b^2 B c d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(7 i a^3 b c C d f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(23 i a^2 A b^2 d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(3 i a^3 b B d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(2 i a^4 C d^2 f^3 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \left(\text{EllipticE} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] - \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \frac{d(-be+af)}{(-bc+ad)f} \right] \right) \right) /$$

$$\left(\sqrt{-\frac{-bc+ad}{d}} (-be+af) \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(5 i b^3 B c d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(10 i a b^2 c C d e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \text{EllipticF} \left[i \text{ArcSinh} \left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(4 i A b^3 d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i a b^2 B d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(6 i a^2 b c d^2 e f \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(4 i A b^3 c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right.$$

$$\left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(i a b^2 B c d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(6 i a^2 b c C d f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) -$$

$$\left(8 i a A b^2 d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

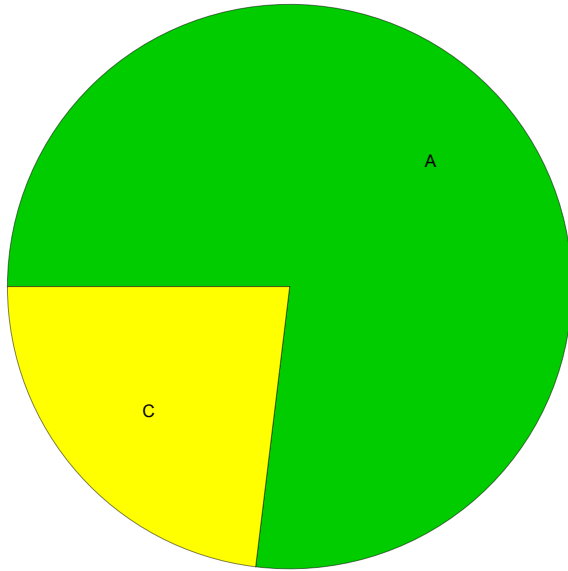
$$\left(3 i a^2 b B d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}} \right], \right. \right.$$

$$\left. \left. \frac{d(-be+af)}{(-bc+ad)f} \right] \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right) +$$

$$\left(2 i a^3 C d^2 f^2 \sqrt{1 - \frac{-bc+ad}{d(a+bx)}} \sqrt{1 - \frac{-be+af}{f(a+bx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-bc+ad}{d}}}{\sqrt{a+bx}}\right]\right], \right. \\ \left. \frac{d(-be+af)}{(-bc+ad)f} \right) / \left(\sqrt{-\frac{-bc+ad}{d}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right)} \right)$$

Summary of Integration Test Results

78 integration problems



- A - 60 optimal antiderivatives
- B - 0 more than twice size of optimal antiderivatives
- C - 18 unnecessarily complex antiderivatives
- D - 0 unable to integrate problems
- E - 0 integration timeouts